

## Bio-History of Kenji Uchino

- **University professor = 40 years**  
Tokyo Tech-10 yrs, Sophia Univ-8 yrs, Penn State-24 yrs
- **Company executive = 21 years**
- **Government Officer = 4 years**
- **Japanese 20 years vs. US 20 years**
- **“One step ahead”**  
Age 40s = Academic initiative  
Age 50s = Entrepreneur  
Age 60s = Program officer
- **“Discover/Inventor”**  
Piezoelectric ML actuators, PMN electrostrictors,  
Relaxor single crystals, Micro motors, Piezoelectric  
transformers, HiPoCS





## Loss Mechanisms in Smart Materials

**Kenji Uchino**  
Int'l Center for Actuators & Transducers  
The Pennsylvania State University

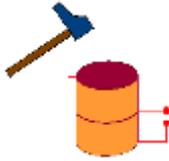


1. Background: Smart Materials
2. Fundamental Loss Equations for Piezoelectrics & Magnetostrictors
3. High Power Characterization System
4. New  $Q_M$  Determination Methods
5. Origin of High Power Performance
6. Summary

Background

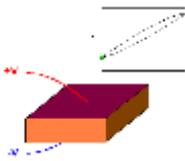
## What's “Piezoelectric Effect”?

**DIRECT PIEZOELECTRIC EFFECT**



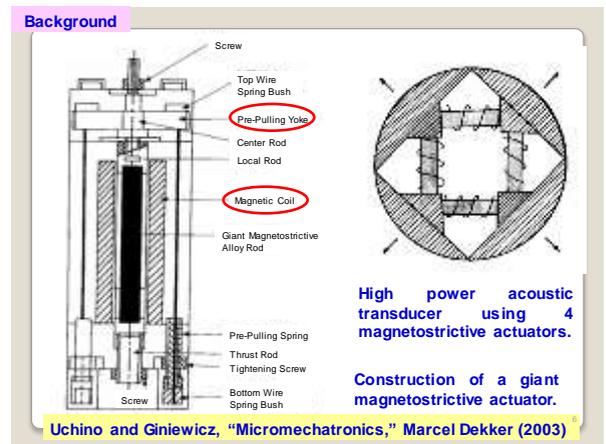
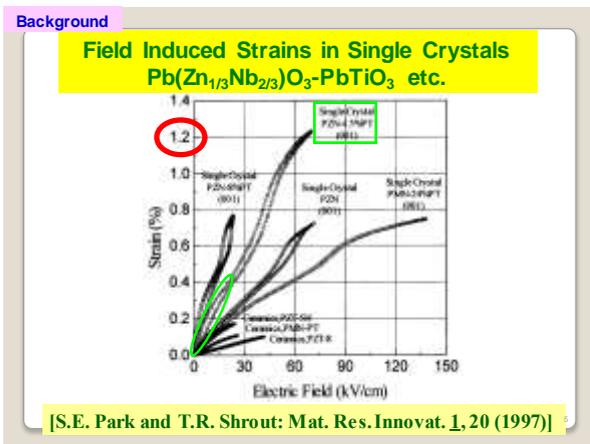
**Igniter  
Microphone  
Pressure Sensor**

**CONVERSE PIEZOELECTRIC EFFECT**



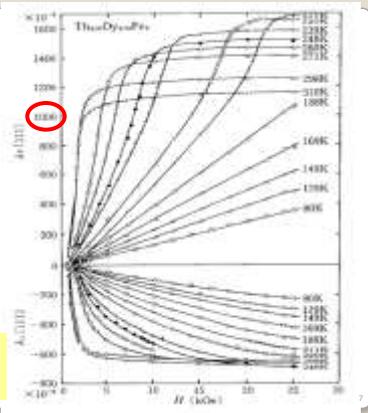
**Clock  
Speaker  
Actuator**



Background

Longitudinally and transversely induced strains in a Terfenol-D for various temperatures.



Uchino and Gniewicz, "Micromechanics," Marcel Dekker (2003)

Background

Electromechanical Coupling Factor  
Typical Piezoelectric PZT

$$k_{33} = 70\% \rightarrow k_{33}^2 = 50\%$$

Input electrical energy 100



Mechanical energy converted 50

Electrical energy stored in a capacitor 49

Loss 1

Dissipated as heat

Energy Transmission Coefficient  $\lambda = (\text{Mech. Output Energy} / \text{Electr. Input Energy}) = (1/4 \sim 1/2) k^2$

Uchino, "Ferroelectric Devices 2<sup>nd</sup> Edit.," CRC Press, NY (2009)

Background

Piezoelectric vs. Electromagnetic Motors

**Potential Strength!**

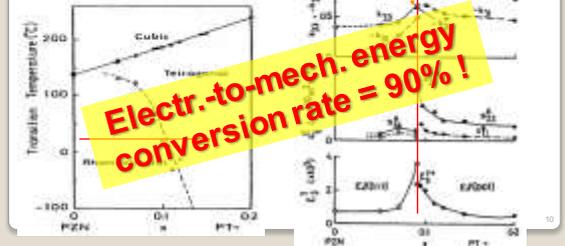
Power	Piezoelectric Efficiency	Electromagnetic Efficiency
30 W	98%	1%
30 kW	70%	1%

\*More suitable to miniaturization  
\*Higher efficiency

Background

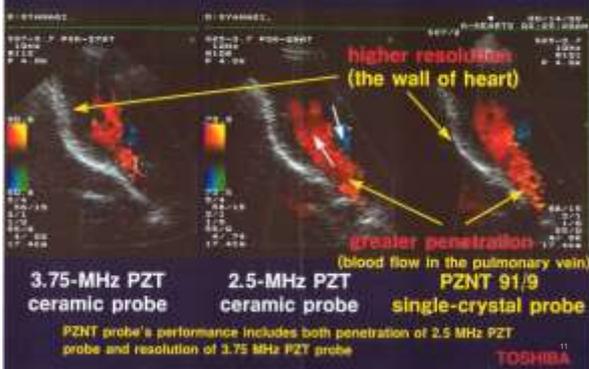
High d and k in  $\text{Pb}(\text{Zn}_{1/3}\text{Nb}_{2/3})\text{O}_3\text{-PbTiO}_3$   
- Crystal Orientation Dependence

[J.Kuwata, K.Uchino and S.Nomura: Ferroelectrics, 37, 579 (1981)]



Background

Comparison of the Doppler mode images



Loss Mechanisms in Smart Materials

Loss Mechanisms in Smart Materials

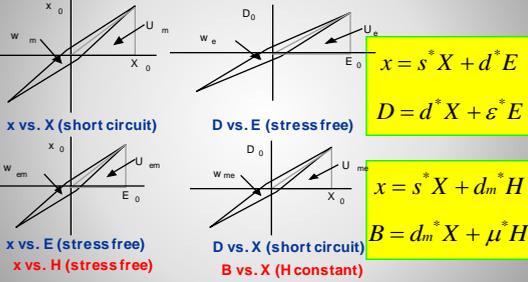
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Fundamental

### Hysteresis Losses

#### Piezoelectric & Piezomagnetic



Three losses: elastic, dielectric and piezoelectric (or piezomagnetic)

Fundamental

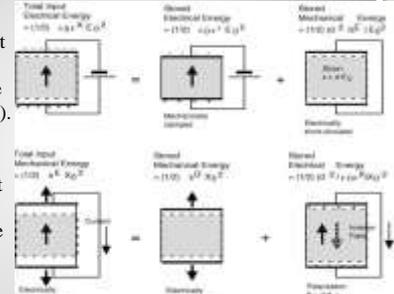
### Intensive vs. Extensive Parameters

**Intensive:**

$\epsilon^X$  - dielectric constant (constant stress);  
 $s^E$  - elastic compliance (constant electric field).

**Extensive:**

$\epsilon^S$  - dielectric constant (constant strain);  
 $s^D$  - elastic compliance (constant electric displacement).



$$\epsilon^S / \epsilon^X = (1 - k^2) \quad k^2 = d^2 / s^E \epsilon^X$$

$$s^D / s^E = (1 - k^2)$$

Fundamental

### Loss Factors

**Intensive loss factors**

$$\epsilon^{X*} = \epsilon^X (1 - j \tan \delta')$$

$$s^{E*} = s^E (1 - j \tan \phi')$$

$$d^* = d (1 - j \tan \theta')$$

**Extensive loss factors**

$$K^{X*} = K^X (1 + j \tan \delta)$$

$$c^{D*} = c^D (1 + j \tan \phi)$$

$$h^* = h (1 + j \tan \theta)$$



Fundamental

### Loss Factors

**Intensive loss factors**

$$\tan \delta' = \left( \frac{1}{1 - k^2} \right) [\tan \delta + k^2 (\tan \phi - 2 \tan \theta)]$$

$$\tan \phi' = \left( \frac{1}{1 - k^2} \right) [\tan \phi + k^2 (\tan \delta - 2 \tan \theta)]$$

$$\tan \theta' = \left( \frac{1}{1 - k^2} \right) [\tan \delta + \tan \phi - (1 + k^2) \tan \theta]$$

**Extensive loss factors**

$$\begin{bmatrix} \tan \delta' \\ \tan \phi' \\ \tan \theta' \end{bmatrix} = K \begin{bmatrix} \tan \delta \\ \tan \phi \\ \tan \theta \end{bmatrix} \quad K = \frac{1}{1 - k^2} \begin{bmatrix} 1 - k^2 & -2k^2 \\ k^2 & 1 - 2k^2 \\ 1 & 1 - 1 - k^2 \end{bmatrix}$$

K is involutory, i.e.  $K^2 = I$ , or  $K = K^{-1}$ .

The conversion relationship between the intensive (prime) and extensive (non-prime) exhibits full symmetry. The eigen values of the matrix K are 1, 1, and -1, and the invariant is

$$(2 \tan \theta' - \tan \delta' - \tan \phi') = -(2 \tan \theta - \tan \delta - \tan \phi)$$

(Loss of  $k^2$ )

Fundamental

Wrong assumption that  $Q_m$  is the same for both Resonance and Antiresonance state!  
**IEEE Standard Measurement on  $Q_m$**

**$k_{31}$  mode**

$$s_{11}^E = 1 / (4 \rho_f^2 f_r^2 l^2)$$

$$K_{31}^2 = \frac{\pi f_{ar}}{2 f_r} \tan \left( \frac{\pi \Delta f}{2 f_r} \right)$$

where,  $K_{31}^2 = \frac{k_{31}^2}{1 - k_{31}^2}$

$$Q_m = \frac{Y_m^{\max} * \pi^2}{8 * \omega_0^3 * C * K_{31}^2}$$

**$k_{33}$  mode**

$$s_{33}^D = 1 / (4 \rho_f^2 f_r^2 l^2)$$

$$K_{33}^2 = \frac{\pi f_r}{2 f_{ar}} \tan \left( \frac{\pi \Delta f}{2 f_{ar}} \right)$$

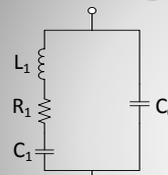
$$K_{33}^2 = \frac{k_{33}^2}{1 - k_{33}^2}$$

$$Q_m = \frac{Y_m^{\max}}{4 * \pi * \Delta f * C}$$

IEEE Standard on Piezoelectricity, ANSI/IEEE Std 176-1987

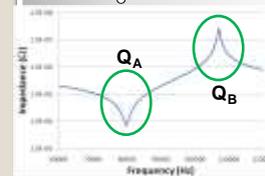
Fundamental

### Quality Factors



$$Q = \frac{\sqrt{L_1 / C_1}}{R_1}$$

IEEE Std.  $Q_A = Q_B = Q_m$ .



Experiment  $Q_A < Q_B$ .

Difference  $\rightarrow \tan \theta'$

**Fundamental Piezoelectric Resonance (Loss-free)**

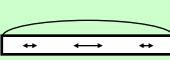
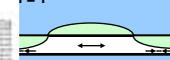


**Damped Motional**

(strain)  $\partial u / \partial x = x_1 = d_{31} E_2 [\sin(\omega(L-x))/v + \sin(\omega x/v)] / \sin(\omega L/v)$   
 (displacement)  $u(L) = \int_0^L x_1 dx = d_{31} E_2 L \tan(\omega L/2v) / (\omega L/2v)$   
 (sound velocity)  $v = 1/\sqrt{\rho s_{11}^E}$   
 $Y = (1/Z) = (iV) = (i/E) \left[ \frac{j\omega L/t}{(1-k_{31}^2)} \left( \frac{d_{31}^2/e^{LC} s_{11}^E}{\tan(\omega L/2v)} \right) \right]$   
 $\epsilon_{33}^{LC} = \epsilon_{33}^* - (d_{31}^2/s_{11}^E) = \epsilon_{33}^* (1-k_{31}^2)$   
 $k_{31}^2 = d_{31}^2/s_{11}^E \epsilon_{33}^*$   
**Piezoelectric Resonance: infinite admittance/zero impedance**  
 $f_R = v/2L = 1/(2L\sqrt{\rho \epsilon_{11}^E})$   
**Antiresonance: zero admittance/infinite impedance**  
 $(\omega_A L/2v) \cot(\omega_A L/2v) = -d_{31}^2/\epsilon_{33}^* s_{11}^E = -k_{31}^2/(1-k_{31}^2)$

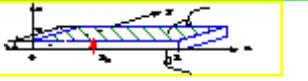
**Fundamental Resonance & Antiresonance Modes**

**Strain Distribution in a Plate**

	Resonance	Antiresonance
<b>m = 1</b>		<b>Low coupling</b>  <b>High coupling</b> 
<b>m = 2</b>		<b>Low coupling</b>  <b>High coupling</b> 

**Note: Stress is zero, but strain is not zero at the plate ends.**

**Fundamental Piezoelectric Resonance (With Losses)**

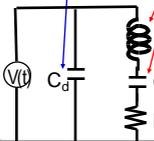


$Y = Y_d + Y_m$   
 $= j\omega C_d \left[ 1 - \frac{j}{(1-k_{31}^2)} [\tan \delta' - k_{31}^2 (2 \tan \theta' - \tan \phi')] \right] + j\omega C_0 k_{31}^2 \left[ \frac{\tan(\omega L/2v^*)}{\omega L/2v^*} \right]$   
 $= j\omega C_d (1 - j \tan \delta) + j\omega C_0 k_{31}^2 \left[ \frac{\tan(\omega L/2v^*)}{\omega L/2v^*} \right] \quad \epsilon^x = \epsilon^x (1-k^2)$   
 $\Omega = \omega L/2v, \Delta\Omega = \Omega - \pi/2 (\ll 1), \Gamma_{31} = k_{31}^2/(1-k_{31}^2)$   
 $v^* = \frac{1}{\sqrt{\rho s_{11}^E (1-j \tan \phi')}} = v (1 + (1/2) j \tan \phi') \quad \frac{1}{\tan(\omega L/2v^*)} = -\Delta\Omega + j(\pi/4) \tan \phi'$   
 $Y_m = j\omega C_d \Gamma_{31} [(1-j)(2 \tan \theta' - \tan \phi')] \left[ \frac{\tan(\omega L/2v^*)}{\omega L/2v^*} \right]$   
 $= j\omega C_d \Gamma_{31} \left[ \frac{1 - j(2 \tan \theta' - \tan \phi')}{(-\Delta\Omega + j(\pi/4) \tan \phi')(\pi/2)(1 - (1/2) j \tan \phi')} \right]$   
 $= j(8/\pi^2) \omega C_d \Gamma_{31} \left[ \frac{1 + j[(3/2) \tan \phi' - 2 \tan \theta']}{-(4/\pi) \Delta\Omega + j \tan \phi'} \right]$

**Fundamental Piezoelectric Resonance (With Losses)**

$Y_d = j\omega C_d (1 - j \tan \delta) = j\omega C_d + \omega C_d \tan \delta$   
 $= j\omega C_d \left[ \frac{\omega C_d}{(1-k_{31}^2)} [\tan \delta' + k_{31}^2 (\tan \phi' - 2 \tan \theta')] \right]$  **Neglect**

$1/Y_m = 1/j(8/\pi^2) \omega C_d \Gamma_{31} \left[ \frac{1 + j[(3/2) \tan \phi' - 2 \tan \theta']}{-(4/\pi) \Delta\Omega + j \tan \phi'} \right]$   
 $= [-(4/\pi) \Delta\Omega + j \tan \phi'] / j(8/\pi^2) \omega C_d \Gamma_{31}$   
 $= j(\pi L/4v \omega_0 C_0 k_{31}^2) \Delta\omega + (\pi^2/8\omega_0 C_0 k_{31}^2) \tan \phi'$   
 $1/Y_m = j\omega L_A + 1/(j\omega C_A + G_A) + R_A \approx j(L_A + 1/\omega_0^2 C_A) \Delta\omega + R_A + G_A'/\omega_0^2 C_A^2$

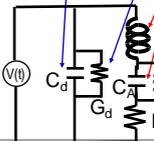


$L_m = (L s_{11}^E / 4v^2 \omega d_{31}^2) / 2 = (\rho/8)(L/t/w)(s_{11}^E/d_{31}^2)$   
 $C_m = 1/\omega_0^2 L_m = (L/n\pi v)^2 (8/\rho)(w/L)(d_{31}^2/s_{11}^E)$   
 $= (8/n^2 \pi^2)(Lw/t)(d_{31}^2/s_{11}^E)$   
 $R_m = \left( \frac{\pi^2}{8\omega_0 C_0 k_{31}^2} \right) \tan \phi_1'$

**Fundamental Piezoelectric Res/Antiresonance (With Losses)**

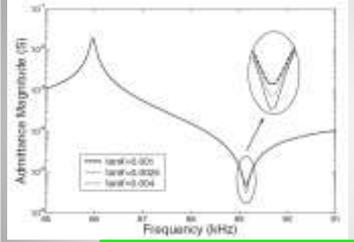
$Y_d = j\omega C_d (1 - j \tan \delta) = j\omega C_d + \omega C_d \tan \delta$   
 $= j\omega C_d \left[ \frac{\omega C_d}{(1-k_{31}^2)} [\tan \delta' + k_{31}^2 (\tan \phi' - 2 \tan \theta')] \right]$

$1/Y_m = 1/j(8/\pi^2) \omega C_d \Gamma_{31} \left[ \frac{1 + j[(3/2) \tan \phi' - 2 \tan \theta']}{-(4/\pi) \Delta\Omega + j \tan \phi'} \right]$   
 $\approx [-(4/\pi) \Delta\Omega + j \tan \phi'] / j(8/\pi^2) \omega C_d \Gamma_{31}$   
 $\approx j(\pi L/4v \omega_0 C_0 k_{31}^2) \Delta\omega + (\pi^2/8\omega_0 C_0 k_{31}^2) \tan \phi'$   
 $1/Y_m = j\omega L_A + 1/(j\omega C_A + G_A) + R_A \approx j(L_A + 1/\omega_0^2 C_A) \Delta\omega + R_A + G_A'/\omega_0^2 C_A^2$



$G_d = \omega C_d \tan \delta_{33} = \left( \frac{\omega C_d}{(1-k_{31}^2)} \right) [\tan \delta_{33}' + k^2 (\tan \phi_1' - 2 \tan \theta_{31}')]$   
 $R_A = \left( \frac{\pi^2}{8\omega_0 C_0 k_{31}^2} \right) \tan \phi_1' \quad G_A' = \omega C_A k_{31}^2 (2 \tan \theta_{31}' - \tan \phi_1') \frac{\tan \Omega_A}{\Omega_A}$   
**Resonance Antiresonance**

**Fundamental Piezoelectric Loss Factor**



**Elastic loss  $\tan \phi'$**   
**Dielectric loss  $\tan \delta'$**   
**Piezoelectric loss  $\tan \theta'$**

- $2 \tan \theta' > (\tan \delta' + \tan \phi')$ :  $Q_A < Q_B$
- $2 \tan \theta' = (\tan \delta' + \tan \phi')$ :  $Q_A = Q_B$
- $2 \tan \theta' < (\tan \delta' + \tan \phi')$ :  $Q_A > Q_B$

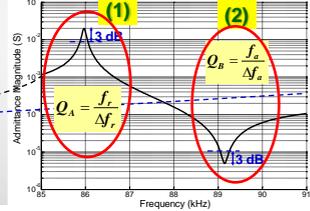
Fundamental

Theoretical Derivation  $k_{31}$  Mode

$$\frac{1}{Q_A} \tan \phi' = \frac{1}{Q_B} = \frac{1}{Q_A} + \frac{2}{1 + \left(\frac{1}{k_{31}} - k_{31}\right)^2 \Omega_b^2} (\tan \delta' + \tan \phi' - 2 \tan \theta')$$

> Because  $Q_B > Q_A$ ,  $2 \tan \theta' > (\tan \delta' + \tan \phi')$ .

(3) Off-resonance dielectric loss



Utilize the difference intentionally !

Fundamental

Anisotropic Losses in Piezoelectric & Piezomagnetic

10 independent parameters for 6mm / ∞mm materials (polycrystalline) – 20 loss factors

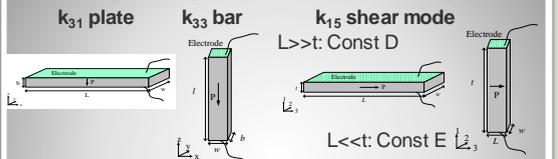
$$\epsilon = \begin{bmatrix} \epsilon_{11} & 0 & 0 \\ 0 & \epsilon_{11} & 0 \\ 0 & 0 & \epsilon_{33} \end{bmatrix} \quad 2$$

$$d = \begin{bmatrix} 0 & 0 & 0 & 0 & d_{15} & 0 \\ 0 & 0 & 0 & d_{15} & 0 & 0 \\ d_{31} & d_{31} & d_{33} & 0 & 0 & 0 \end{bmatrix} \quad 3$$

$$\epsilon = \begin{bmatrix} \epsilon_{11} & \epsilon_{12} & \epsilon_{13} & 0 & 0 & 0 \\ \epsilon_{12} & \epsilon_{11} & \epsilon_{13} & 0 & 0 & 0 \\ \epsilon_{13} & \epsilon_{13} & \epsilon_{33} & 0 & 0 & 0 \\ 0 & 0 & 0 & \epsilon_{44} & 0 & 0 \\ 0 & 0 & 0 & 0 & c_{44} & 0 \\ 0 & 0 & 0 & 0 & 0 & \frac{c_{11} - c_{12}}{2} \end{bmatrix} \quad 5$$

Fundamental

Quality Factor Anisotropy



$$Q_{A,31} = \frac{1}{\tan \phi_{11}'} \frac{1}{Q_{B,31}} = \frac{1}{Q_{A,31}} + \frac{2}{1 + \left(\frac{1}{k_{31}} - k_{31}\right)^2 \Omega_{B,31}^2} (\tan \delta_{33}' + \tan \phi_{11}' - 2 \tan \theta_{31}')$$

$$Q_{B,33} = \frac{1}{\tan \phi_{33}'} \frac{1}{Q_{A,33}} = \frac{1}{Q_{B,33}} - \frac{2}{k_{33}^2 - 1 + \Omega_{A,33}^2 / k_{33}^2} (2 \tan \theta_{33} - \tan \delta_{33} - \tan \phi_{33})$$

$$Q_{B,15}^D = \frac{1}{\tan \phi_{35}'} \frac{1}{Q_{A,15}^D} = \frac{1}{Q_{B,15}^D} - \frac{2}{k_{15}^2 - 1 + \Omega_{A,15}^2 / k_{15}^2} (2 \tan \theta_{15} - \tan \delta_{11} - \tan \phi_{35})$$

$$Q_{A,15}^E = \frac{1}{\tan \phi_{25}'} \frac{1}{Q_{B,15}^E} = \frac{1}{Q_{A,15}^E} + \frac{2}{1 + \left(\frac{1}{k_{15}} - k_{15}\right)^2 \Omega_{B,15}^2} (\tan \delta_{11}' + \tan \phi_{35}' - 2 \tan \theta_{15}')$$

Fundamental

Loss Anisotropy Determination

Material parameters of ∞mm/6mm:

16 loss factors can be derived.  
 $\epsilon_{33}^X, \epsilon_{11}^X, \epsilon_{33}^E, \epsilon_{11}^E;$   
 $s_{11}^E, s_{12}^E, s_{13}^E, s_{33}^E, s_{44}^E, s_{11}^D, s_{12}^D, s_{13}^D, s_{33}^D, s_{44}^D;$   
 $d_{31}, d_{33}, d_{15}, h_{31}, h_{33}, h_{15}.$

Loss factors of APC 841 (~10<sup>-3</sup>) from k<sub>31</sub> and k<sub>33</sub> modes

$\tan \phi_{11}'$	$\tan \phi_{33}'$	$\tan \delta_{33}'$	$\tan \theta_{31}'$	$\tan \theta_{33}'$
0.77	0.90	3.5	3.7	2.5
$\tan \phi_{11}$	$\tan \phi_{33}$	$\tan \delta_{33}$	$\tan \theta_{31}$	$\tan \theta_{33}$
0.44	0.54	3.1	0.25	1.5

- a) Piezoelectric loss factors are not small:  $\tan \theta' > (1/2)(\tan \delta' + \tan \phi')$
- b) Intensive losses are larger than the Extensive losses.
- c) Loss anisotropy

Uchino, Zhuang and Ural, J. Adv. Dielectrics, 1(1), 17-31 (2011).

Fundamental

Piezo vs. Magnetostriction

Piezoelectric K33 Mode

$$Q_{B,33} = \frac{1}{\tan \phi_{33}'} \frac{1}{Q_{A,33}} = \frac{1}{Q_{B,33}} - \frac{2}{k_{33}^2 - 1 + \Omega_{A,33}^2 / k_{33}^2} (2 \tan \theta_{33} - \tan \delta_{33} - \tan \phi_{33})$$

Magnetostrictive K33 Mode

$$Q_A = \frac{1}{\tan \phi_m'}$$

$$\frac{1}{Q_B} = \frac{1}{Q_A} + \frac{2}{1 + \left(\frac{1}{k_{33}} - k_{33}\right)^2 \Omega_b^2} (\tan \delta_m' + \tan \phi_m' - 2 \tan \theta_m')$$

Fundamental

Piezomagnetic Losses

- (1) Three losses types-losses factors  
 $s_m^H = s^H (1 - j \tan \phi_m')$  – Mechanical loss –  $c^B = c^B (1 + j \tan \phi_m)$   
 $d_m^* = d_m (1 - j \tan \theta_m')$  – Piezomagnetic loss –  $h_m^* = h_m (1 + j \tan \delta_m)$   
 $\mu^x = \mu^x (1 - j \tan \delta_m')$  – Magnetic loss –  $v^x = v^x (1 + j \tan \theta_m)$

(2) Impedance of Magnetostrictors

$$Z = j\omega \frac{\pi^2 N^2}{l} \mu_{33}^2 \left( 1 + \frac{k_{33}^2 \tan(\omega l / 2\nu)}{1 - k_{33}^2 (\omega l / 2\nu)} \right)$$

(3) Mechanical Quality factors -losses factors

$$Q_A = (\tan \phi_m')^{-1}$$

$$\frac{1}{Q_B} = \frac{1}{Q_A} + \frac{2}{1 + \left(\frac{1}{k_{33}} - k_{33}\right)^2 \Omega_b^2 / k_{33}^2} (2 \tan \theta_m - \tan \delta_m - \tan \phi_m)$$

(4) Intensive and extensive losses factors

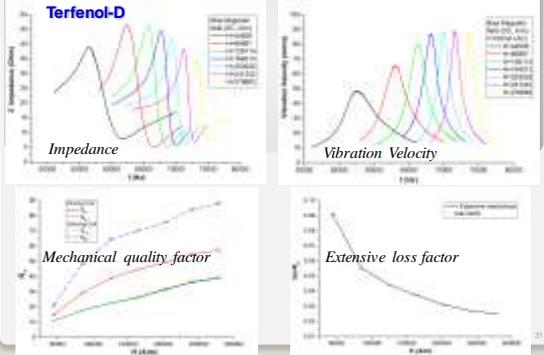
$$(-\tan \delta_m' - \tan \phi_m' + 2 \tan \theta_m') = (\tan \delta_m + \tan \phi_m - 2 \tan \theta_m)$$

$$\begin{bmatrix} \tan \delta_m' \\ \tan \phi_m' \\ \tan \theta_m' \end{bmatrix} = K \begin{bmatrix} \tan \delta_m \\ \tan \phi_m \\ \tan \theta_m \end{bmatrix} \quad K = \frac{1}{1 - k_{33}^2} \begin{bmatrix} 1 & k_{33}^2 & -2k_{33}^2 \\ k_{33}^2 & 1 & -2k_{33}^2 \\ 1 & 1 & -1 - k_{33}^2 \end{bmatrix}$$

Fundamental

### Piezomagnetic Losses

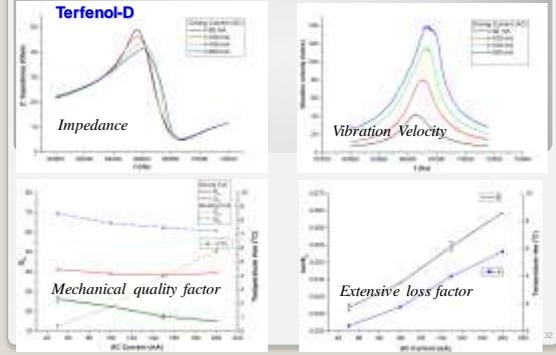
Dependence of losses factors on **Bias magnetic field (DC)**



Fundamental

### Piezomagnetic Losses

Dependence of losses factors on **Driving magnetic field (AC)**



Fundamental

### Piezomagnetic Losses

(1) Magnetic phase lag:  $\delta'_m = 2.54^\circ$ ,  $\tan \delta'_m = 0.044$  **Terfenol-D**

	Intensive losses factors		Extensive losses factors	
<b>Elastic loss</b>	$\tan \phi'_m$	0.0657	$\tan \theta'_m$	0.0556
<b>Magnetic loss</b>	$\tan \delta'_m$	0.0440	$\tan \delta'_m$	0.0338
<b>Piezomagnetic loss</b>	$\tan \theta'_m$	0.0893	$\tan \theta'_m$	0.0103

(2) Magnetic phase lag:  $\delta'_m = 3.90^\circ$ ,  $\tan \delta'_m = 0.068$

	Intensive losses factors		Extensive losses factors	
<b>Elastic loss</b>	$\tan \phi'_m$	0.0622	$\tan \theta'_m$	0.0556
<b>Magnetic loss</b>	$\tan \delta'_m$	0.0680	$\tan \delta'_m$	0.0614
<b>Piezomagnetic loss</b>	$\tan \theta'_m$	0.0875	$\tan \theta'_m$	0.0361

**Piezoelectric loss ~ 0.3%**  
**Piezomagnetic loss ~ 9%**

Conditions: (a) DC bias magnetic field  $H = 126114 \text{ A/m}$ ;  
 (b) AC driving Current:  $I = 100 \text{ mA}$

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High Power

### High Power Piezo-Devices

**Piezoelectric Devices**

**Heat Generation**

↓

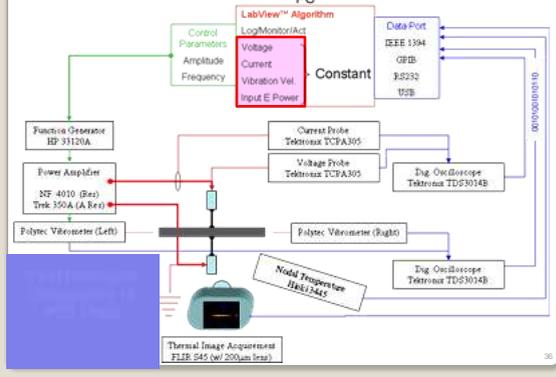
- Miniaturization
- High power density

← **Low Loss**

High Power

### HiPoCS (ICAT/PSU)

(High Power Characterization System)



High Power

PIEZO-RESONANCE METHODS

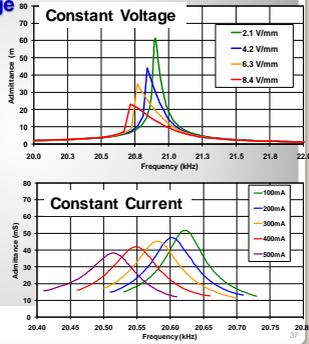
PZT-8 at High Drive Voltage

- The current jump phenomenon prevents an accurate measure of  $Q_M$ .

Nonlinear elastic properties

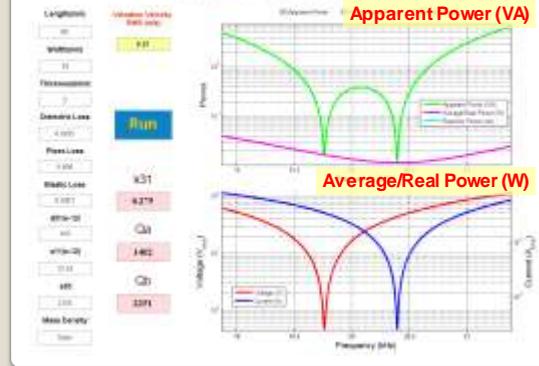
- Rapid changes in voltage are required to maintain constant current in a high Q device at resonance.
- Thermal effects can interfere with the measurement.

(Courtesy by Michael R. Thibeault)



High Power

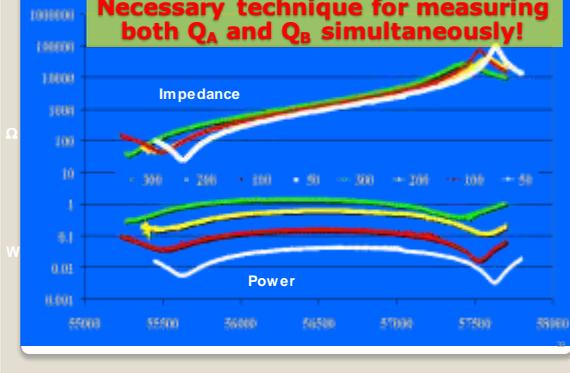
Constant Vibration Velocity Sweep



High Power

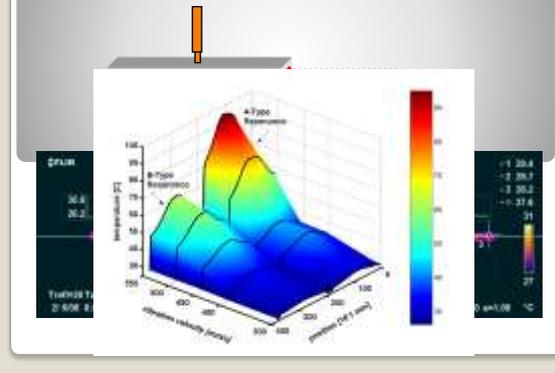
Frequency Sweep @ Vibration Velocity Constant

Necessary technique for measuring both  $Q_A$  and  $Q_B$  simultaneously!



High Power

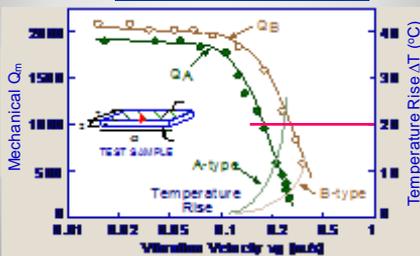
Thermal Behavior @ Vibration Velocity Constant



High Power

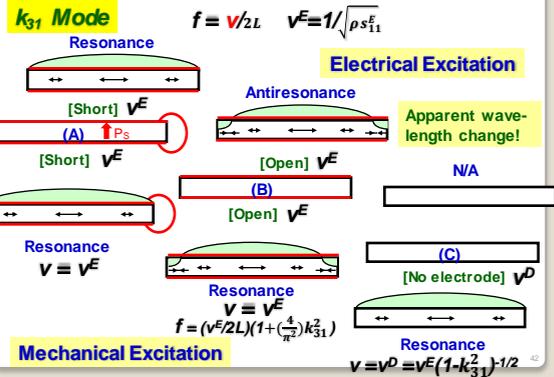
Losses at the Resonance Frequency

Max vibration velocity for the commercialized PZT is 0.3 m/s



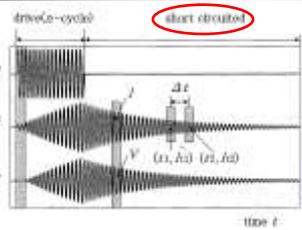
High Power

Resonance & Antiresonance Modes



High Power

### Burst Mode Measurement (Resonance)



$$\beta = \frac{\ln \left( \frac{I_{t1}}{I_{t2}} \right)}{\Delta t}$$

$$Q_A = \frac{c}{2\beta}$$

10-100 Burst count  
→ No temp rise

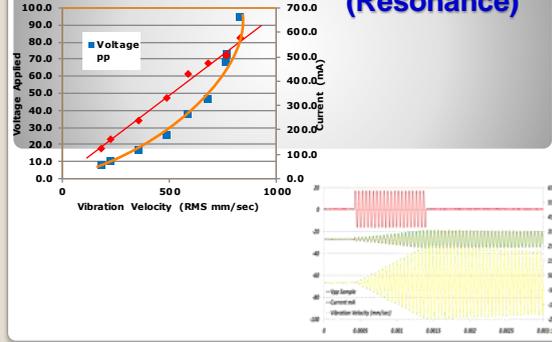
Short Circuit → E const →  $Q_A$

Open Circuit → D const →  $Q_B$

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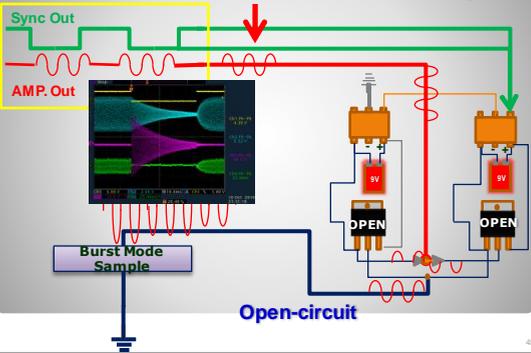
High Power

### Vibration Velocity Control with Burst (Resonance)



High Power

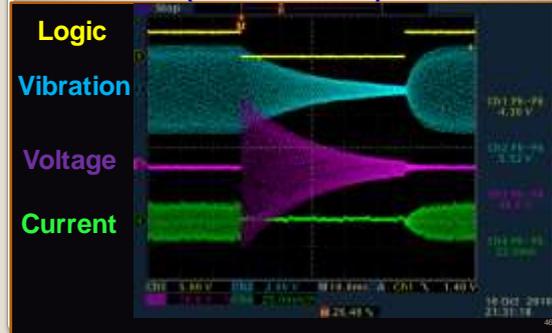
### Antiresonance Switch Principle



45

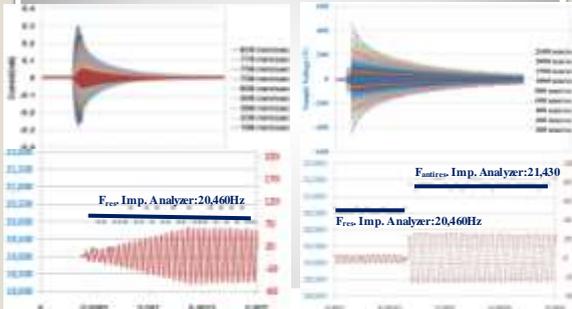
High Power

### Burst Mode Measurement (Antiresonance)



High Power

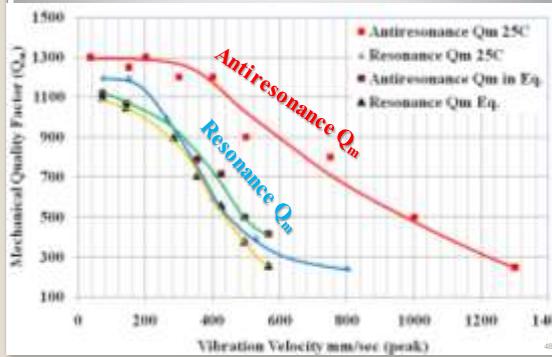
### Burst Mode Measurement Short-circuit Open-circuit



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High Power

### $Q_M$ Map via Burst Mode



PENNSYLVANIA STATE UNIVERSITY **ICAT**

## Loss Mechanisms in Smart Materials

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New Method

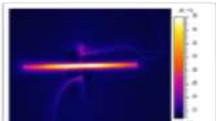
## How to Determine $Q_m$

$Q_{is} = 2\pi \frac{\text{Energy Stored/Cycle}}{\text{Energy Lost/Cycle}}$  **At Res/Antires frequencies**

1. Admittance/Impedance Spectra
  - Under constant voltage
  - Under constant current
  - Under constant vib. velocity
  - Under constant power $Q_m = \left( \frac{\omega_0}{\Delta\omega_{3dB}} \right)$
2. Precise Input Electric Energy  $Q_{m,i} = 2\pi f \frac{\frac{1}{2}\rho V_{RMS}^2}{P_d/(Lwt)}$
3. Precise Temperature Distribution Profile
 

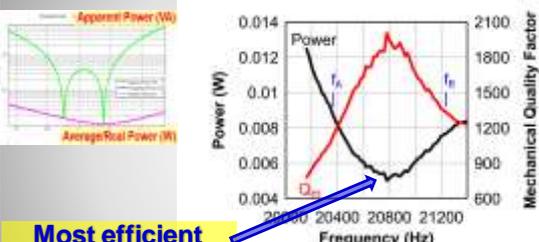
**At any frequencies**  $Q_m = 2\pi f \left( \frac{\rho V_{RMS}^2}{h_g} \right)$

Elevated Temperature of Piezoelectric Ceramic under Resonance Excitation



New Method

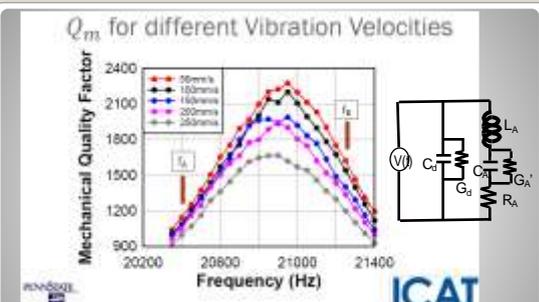
## $Q_m$ from Electrical Power



**Most efficient driving frequency**

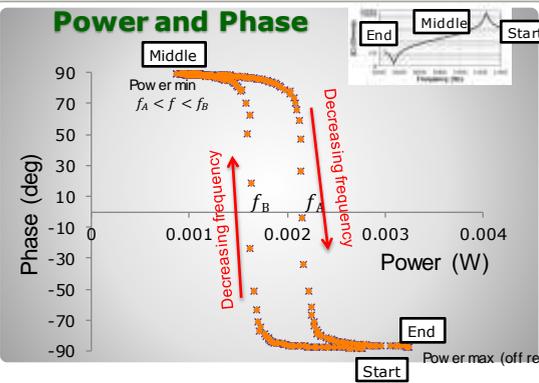
$$Q_{m,i} = 2\pi f \frac{\frac{1}{2}\rho V_{RMS}^2}{P_d/(Lwt)}$$

## $Q_m$ for different Vibration Velocities



Quality Factor Maximum:  $(\omega^4 - \omega_a^2\omega_d^2)(\omega^2 - \omega_a^2) + \omega_a^2\omega_c^4 = 0$   
where  $\omega_c^2 = \omega_a^2 \tan\phi' + (\omega_a^2 - \omega_d^2)(\tan\phi' + \tan\delta' - 2\tan\theta')$

## Power and Phase



Power min  $f_A < f < f_B$

Power max (off res)

PENNSYLVANIA STATE UNIVERSITY **ICAT**

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Loss Mechanism

### Four Types of Losses in Piezoelectrics

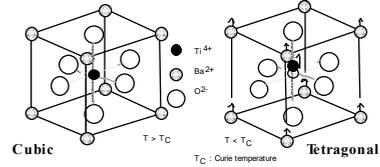
- (1) Domain wall motion
- (2) Fundamental lattice contribution, which should also happen in domain free monocrystals
- (3) Microstructural contribution, which occurs typically in polycrystalline samples
- (4) Conductivity contribution in highly-ohmic samples

In typical piezoelectric ceramics, the loss due to the domain wall motion significantly exceeds the other three types.

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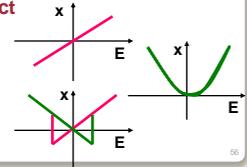
Loss Mechanism

### Crystal Structure of BaTiO<sub>3</sub>



### Origins of Field Induced Strain

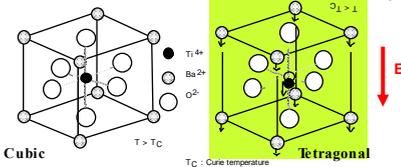
1. Converse piezoelectric effect  
 $x = d E$
2. Electrostrictive effect  
 $x = M E^2$
3. Strain associated with polarization reversal



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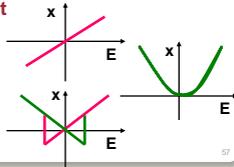
Loss Mechanism

### Crystal Structure of BaTiO<sub>3</sub>



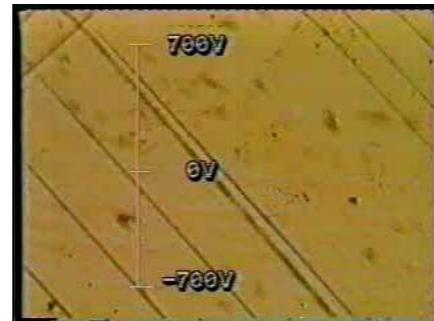
### Origins of Field Induced Strain

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Loss Mechanism

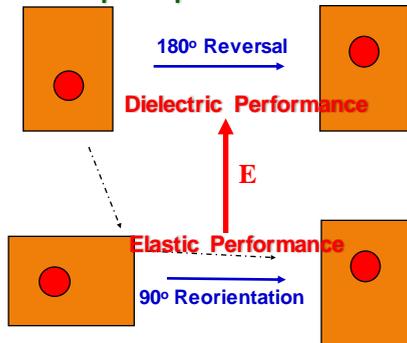


Domain Dynamics in BT

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Loss Mechanism

### Microscopic Aspects of Domain Motion



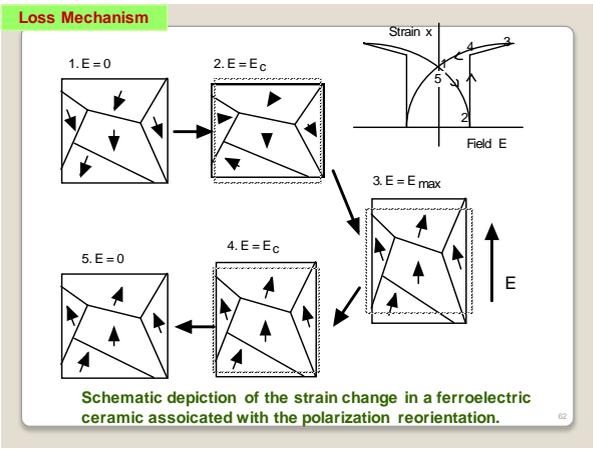
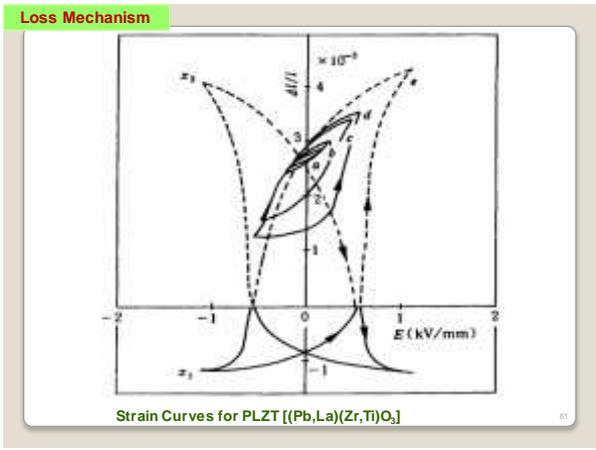
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Loss Mechanism

### Microscopic Origins of the Losses

	Electric Field	Stress
dielectric $\tan \delta$		
mechanical $\tan \phi$		
piezoelectric $\tan \theta$		

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**Loss Mechanism**

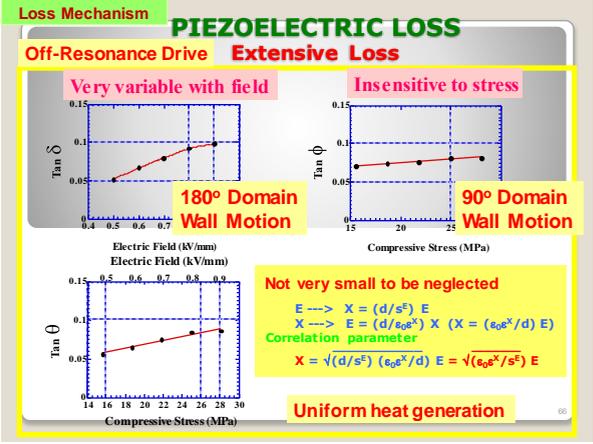
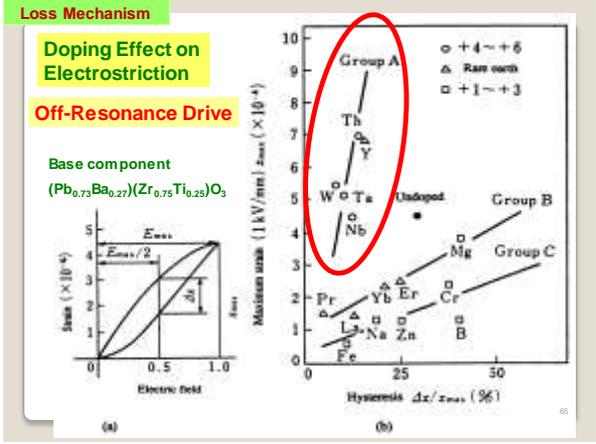
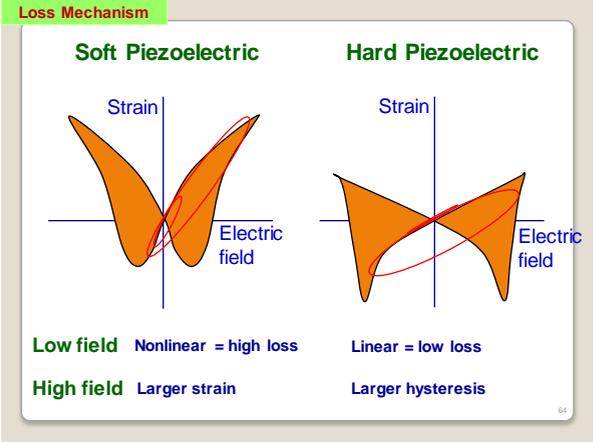
### HARD & SOFT MATERIALS AND LOSS

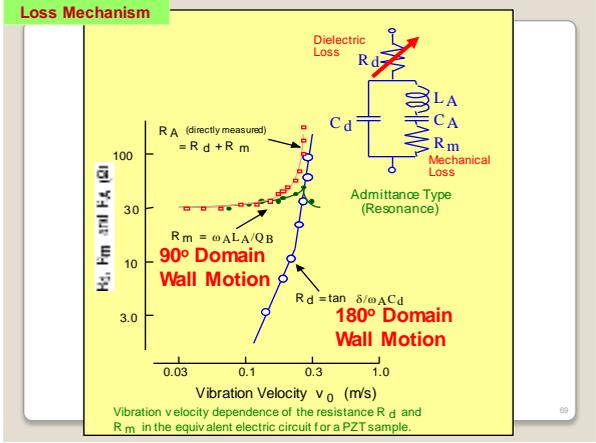
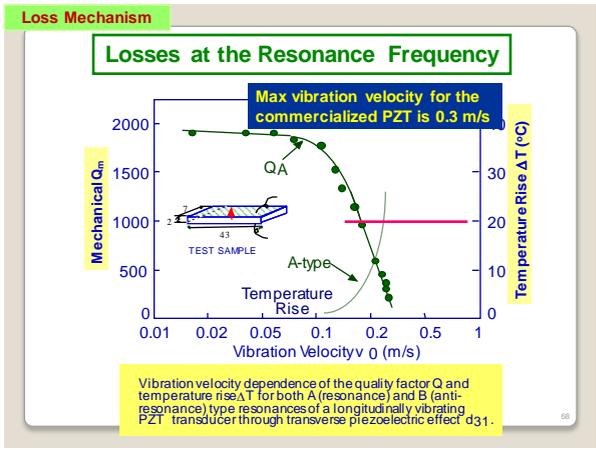
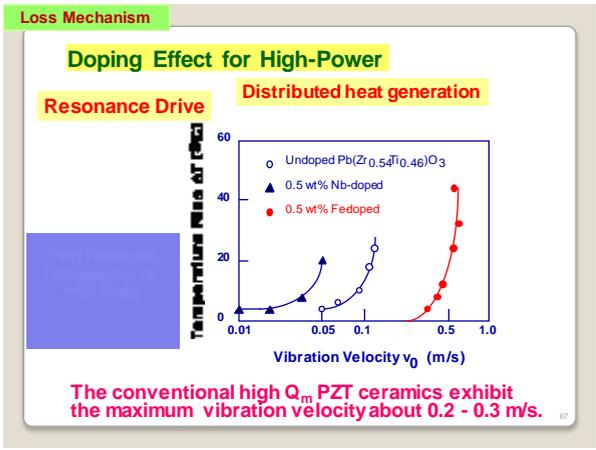
	d	k	Q <sub>m</sub>	Off-Resonance Application	Resonance Application
Electro-strictor (PMN)	High	High	Low	High displacement *(under DC bias)	High displacement No hysteresis
Soft Piezo (PZT-5H)	High	High	Low	High displacement ( $\Delta L = dEL$ )	heat generation
Hard Piezo (PZT- 8)	Low	Low	High	*Low strain	High AC displacement ( $\Delta L \propto Q_m dEL$ )

Motor  
Heat generation

Half  
Hundred times

\* Demerit





**Loss Mechanism**

### Defect distribution and mobility have important influences on materials properties

#### Doping Effects

(S. Takahashi, N.W. Thomas, Imry and Ma)

- ◆ Donor doping  $\Rightarrow$  Lead vacancies, Immobile quenched random field type defect  $\Rightarrow$  Domain motion facilitated
- ◆ Acceptor doping  $\Rightarrow$  Oxygen vacancies, Mobile type Defect  $\Rightarrow$  Domain wall pinning

**HARD PZT**  
 Domain wall pinning  
 Internal bias effect  $\Rightarrow$  P and d decrease  
 $Q_m$  increase

**Loss Mechanism**

### Domain Wall Pinning by Crystal Deficiencies

#### Domain Wall Pinning

**Gauss Law:  $\text{div } P = \sigma$**

(a) Easy to move

(b) Stable

#### Crystal Deficiencies

O Vacancy: easy to move

A Vacancy: prohibited

(a) Acceptor Doping

(b) Donor Doping

**Loss Mechanism**

### Pinning Effects

150°C was reported to be the temperature near which mobile defects begin to move.

PKZT, Q. Tan and D. Viehland, Philosophical Magazine, 1997

**Loss Mechanism**

### Internal Bias

- A shift of P-E curves along field axis without application of DC electric field (E).
- Stabilizing Effect
- Similar to Real Electric Field (G. Arlt and H. Neumann, Ferroelectrics, 1988)

**BaTiO<sub>3</sub>-Ni (G. Arlt and H. Neumann, Ferroelectrics, 1988)**

**Loss Mechanism**

### Time Vs. P-E Curves

**Soft PZT**  
Max  $v_0 = 1.0 \text{ m/s}$

**Hard PZT**  
Max  $v_0 = 0.6 \text{ m/s}$

**Positive Internal Bias Field**

- PZT-PSM-Yb Fresh
- PZT-PSM-Yb 48 hr
- PZT-PSM-Yb Aged

**Loss Mechanism**

### Time Dependence of Electromechanical Characterization

**Even hard materials exhibit very low  $Q_m$  just after the poling.**

**Contradictory to the conventional domain wall pinning effect**

**Loss Mechanism**

### Model: Introduction of Bias Field

**Local field**  
 $E^{\text{local}} = (\gamma/3\epsilon_0)P$

**Loss Mechanism**

### Drastic dielectric loss change

**Electric field dependence of the domain volume fraction of 180° reversal (a) and of 90° reorientation (b). Notice the deviation of the zero fraction points, I and G, between 180° and 90°. [Uchida-Ikeda Model]**

**Loss Mechanism**

### High Power Characteristics in Pb-Free Piezoelectric Rectangular Plate

**hard-PZT**

**Constant Vibration Velocity ( $v_{rms}$ )**

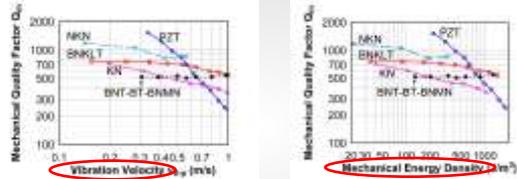
- Mechanical quality factor ( $Q_m$ ) drops
- $v_{max} = 0.8 \text{ m/s}$  &  $0.9 \text{ m/s}$  measured

**Max Vib. Velocity in NKN is higher than PZT!**

**Vibration Velocity (m/s)**

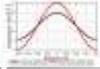
**Dimensions: 10 mm x 0.5 mm x 3 mm**

### Mechanical Energy Density as a Figure of Merit



$$\text{Mech. Energy Density} = (1/2)\rho V_{rms}^2$$

Light mass-density Pb-free piezoelectrics need to vibrate much larger for generating the same mechanical energy.



#### Thermal Conductivity

Thermal Properties	$\kappa$ (W/mK)	$\kappa$ (W/mK)
Hard-PZT	0.42	1.25
NKN-Cu	0.58	3.10

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## SUMMARY

1. Phenomenological equations derived for piezoelectrics & magnetostrictors: dielectric, elastic and piezoelectric losses; magnetic, elastic and piezomagnetic losses. **Coupling losses are significant (not negligible).**
2. Three losses can be determined from  $Q_M$  values for the **resonance and antiresonance ranges.**
3. Three high-power characterization methods (HiPoCS) for determining  $Q_M$ 's; (1) admittance spectra under a **constant vibration velocity**, (2) **burst mode** (mechanical drive) to eliminate the heat generation, (3) precise input electric power.
4. Losses in magnetostrictors: 10 times of losses in piezoelectrics
5. Most efficient driving frequency exists between the resonance and antiresonance frequencies.
6. High power origin: (1) Domain wall pinning, (2) Internal bias. **Internal bias** generation due to **oxygen vacancy diffusion** seems to be the best explanation.
7. High power FOM: Mech. Energy Density =  $(1/2)\rho V_{rms}^2$

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## Loss Mechanisms in Smart Materials

# END

## Thank you!

[www.psu.edu/dept/ICAT](http://www.psu.edu/dept/ICAT)

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E-mail: [kenjiuchino@psu.edu](mailto:kenjiuchino@psu.edu); Phone: 814-863-8035, Fax: 814-865-2326

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