



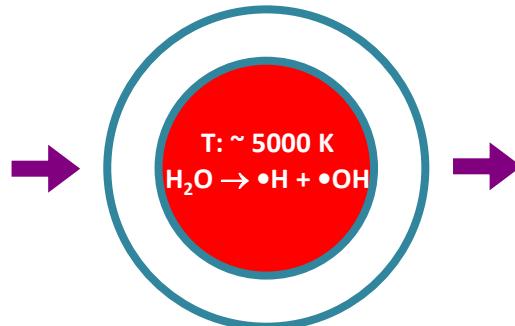
THE OHIO STATE UNIVERSITY

# A Multi-Stepped Ultrasonic Horn for Industrial Scale Processes

Zongsu Wei, James A Kosterman,  
Ruiyang Xiao, Gim-Yang Pee, Meiqiang Cai, Linda K Weavers

April 20<sup>th</sup>, 2015  
Washington D.C.

# Sonochemistry in Remediation



Transient cavitation bubble

- Oxidation
- Thermolysis



Micro-jet , micro-streaming  
pitting, collision

- Desorption
- Accessibility

## *Cavitation*

# Scale Up Sonochemical Treatment

---

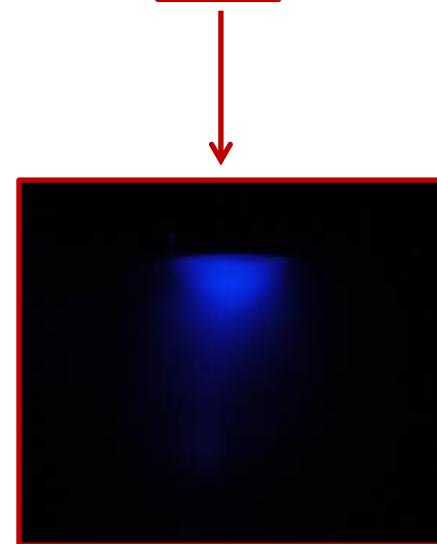
- Increase bioavailability, initiate degradation reaction, and enhance reaction rate
- Improve heat and mass transfer
- Designs in both ultrasonic devices and sono-reactors

# Typical Ultrasonic Horn

- Shrinking dimension
- Small energy-emitting surface
- Concentrated cavitation volume
- Reduced contaminant removal



- **Low energy efficiency (13.3-28.1%)**
- **Scaling-up is very difficult!**



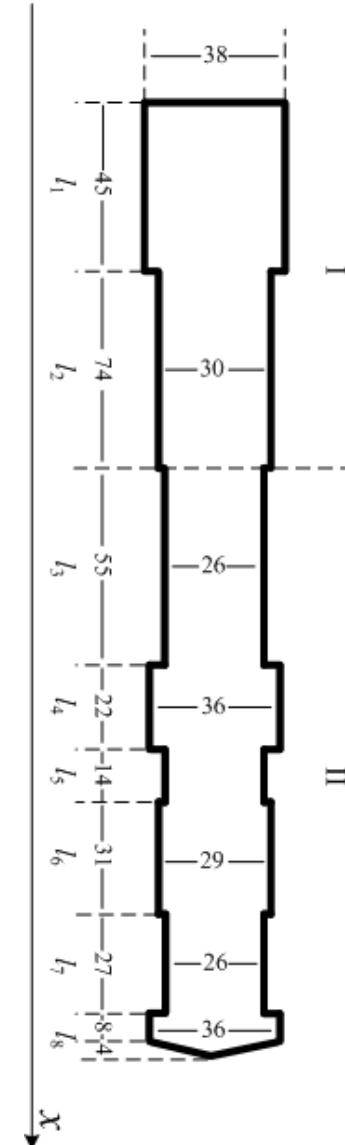
# Objectives

---

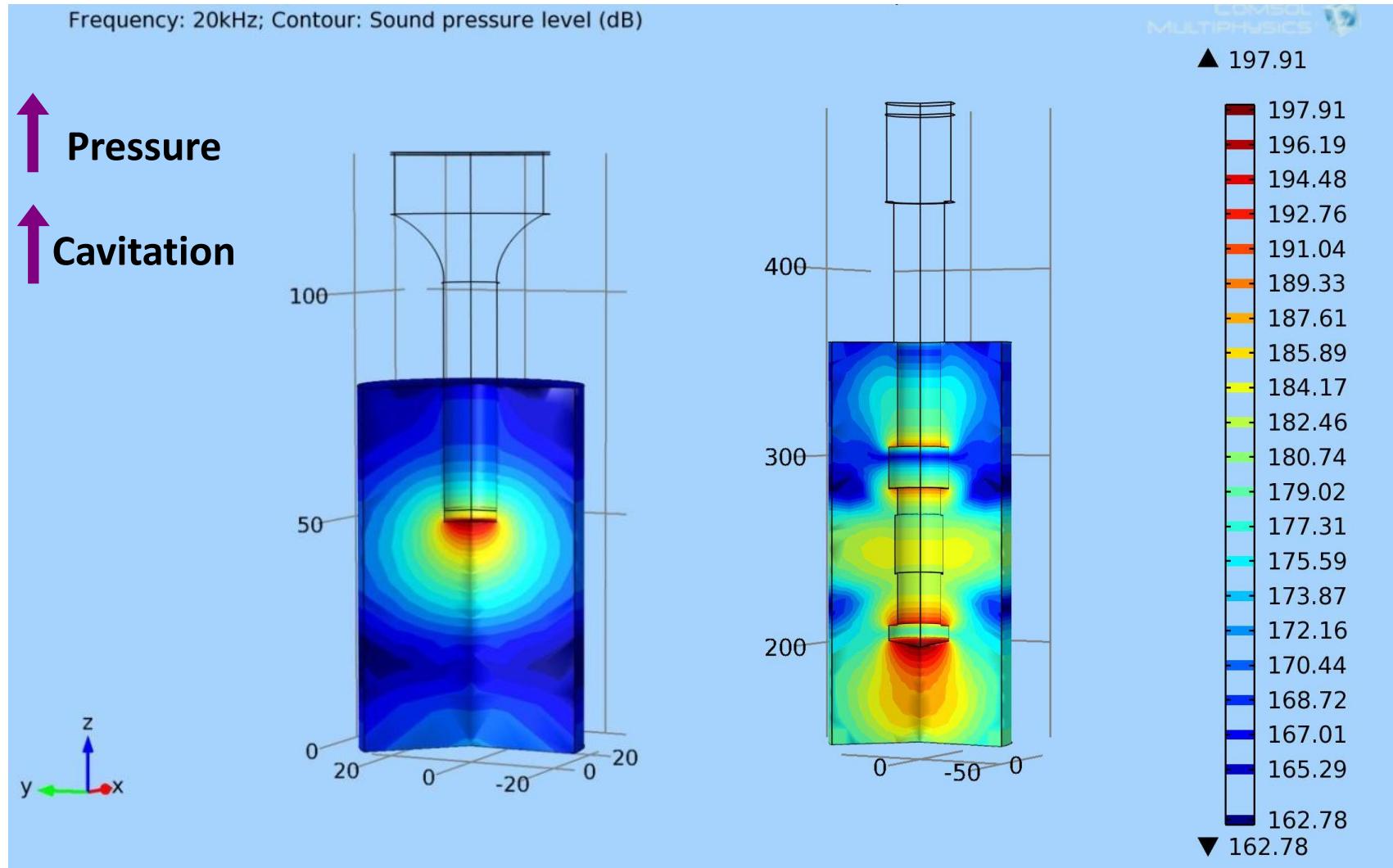
- To design an improved horn configuration
- To characterize the designed horn
  - physical methods
  - chemical methods
- To evaluate large-scale application
  - hydrophone mapping
  - optimal size of sono-reactor

# Design Steps

1. General requirements
  - resonance
2. Specific requirements
  - shape
3. Design principles
  - dynamic wave equation
  - equivalent circuit model
4. Verification using simulation
  - finite element analysis (FEA)
  - COMSOL Multiphysics



# COMSOL Simulation



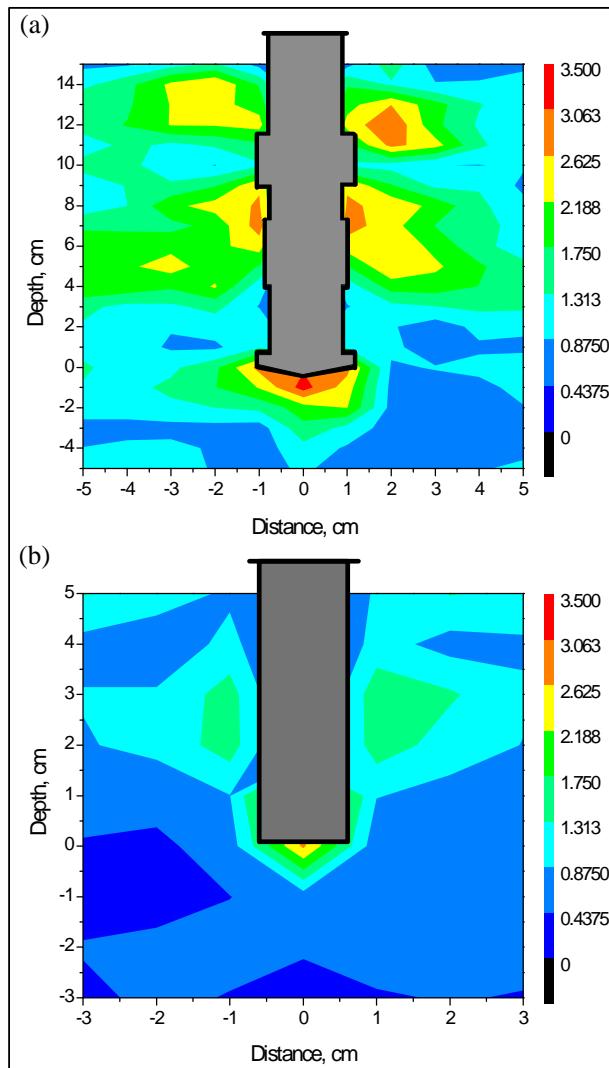
# Horn Characterization



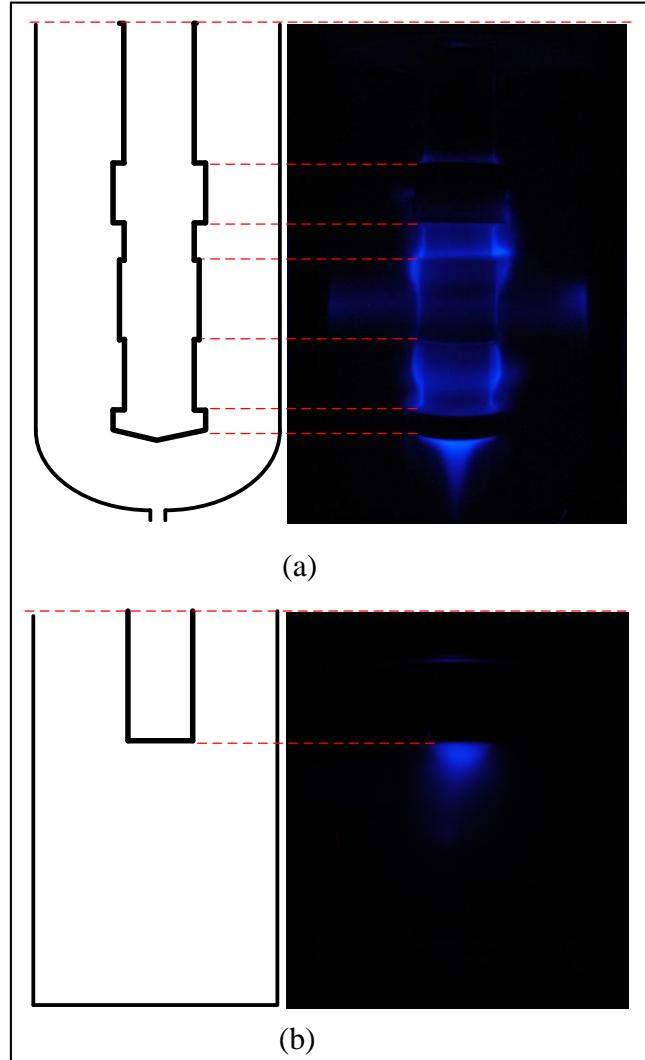
Designed horn



Typical horn



Hydrophone Measurements



Sonochemiluminescence (SCL)

# Comparison - Energy, Cavitation, and Degradation

Horn	Energy efficiency (%)	<sup>a</sup> Zero-order •OH formation rate constant ( $\mu\text{M}/\text{min}$ )	<sup>b</sup> First-order degradation rate constants (1/min)
	31.5	0.36	0.022
	13.3	0.09	0.012

<sup>a</sup> Initial concentration of terephthalate acid = 2mM; <sup>b</sup> initial concentration of phenanthrene = 10 $\mu\text{M}$

# Energy Cost Estimation

Horn type	Typical	Designed
$k, \text{ min}^{-1}$	0.0158	0.0217
$t_{90}, \text{ min}$	145.5	106.1
$P_{\text{elec}}, \text{kW}$	0.275	1.000
$V, \text{ L}$	0.04	1.25
$C_0, \mu\text{M}$	10.0	10.0
$\text{EE/O}$	$1.67 \times 10^4$	$1.41 \times 10^3$
Electricity price, \$ kWh <sup>-1</sup>	0.08	0.08
Cost, \$ per 1000L	1,330	113

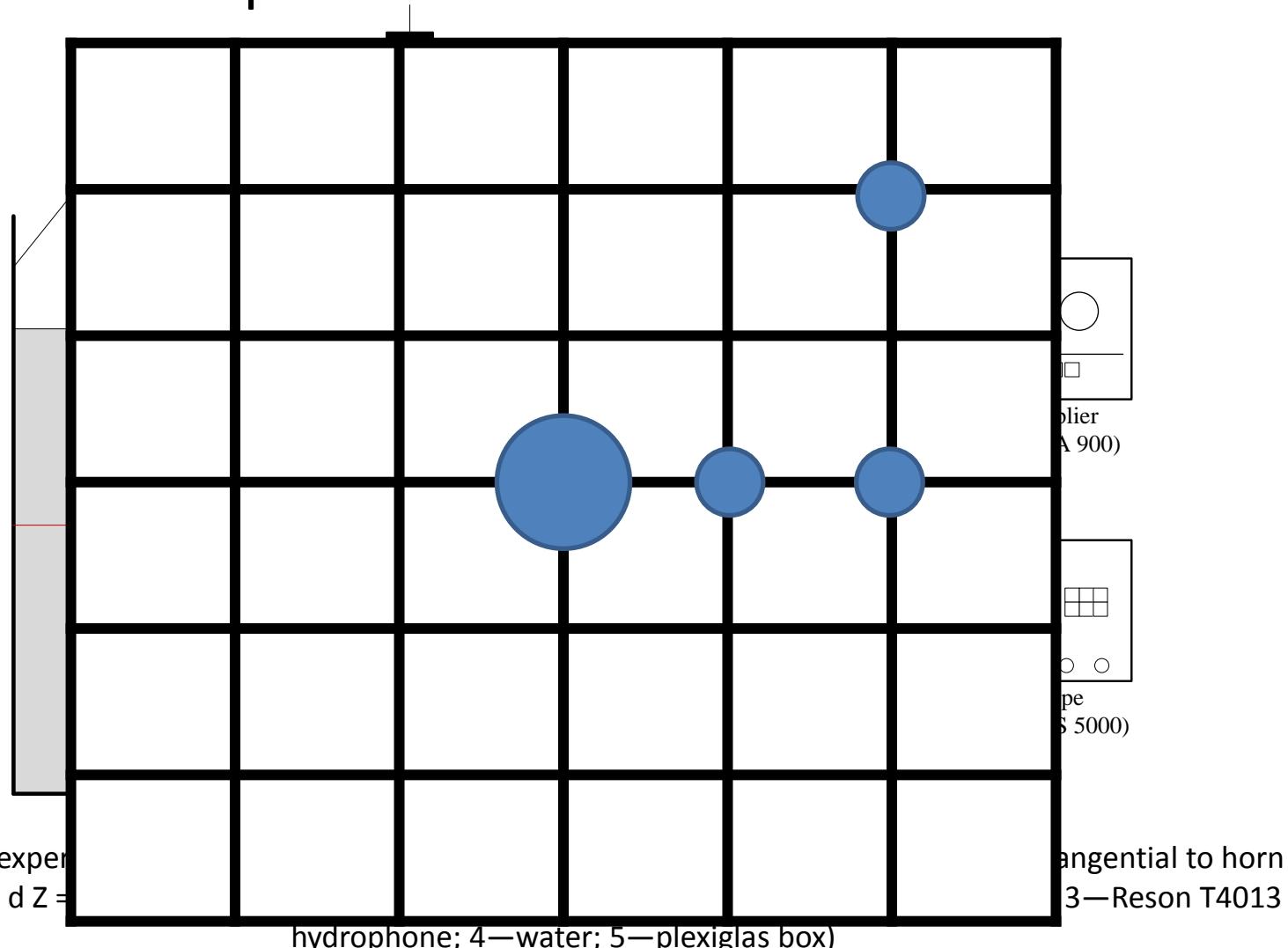
8.5%

- Phenanthrene (first-order degradation)
- 90% removal
- \$0.08/kWh

$$\text{EE/O} = \frac{P_{\text{elec}} \times t_{90} \times 1000}{V \times 60 \times \log(C_0/C)}$$

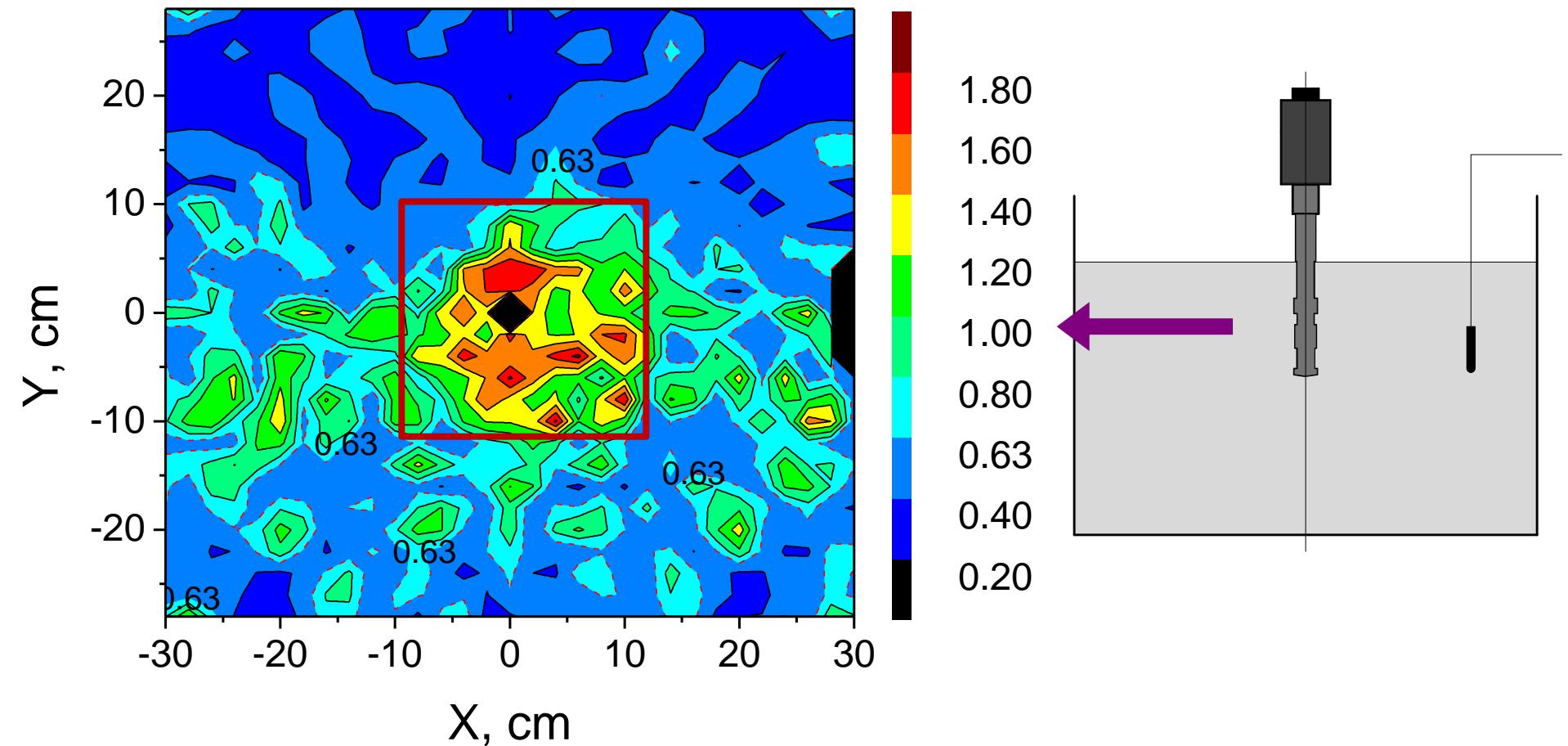
# Large-Scale Reactor Design

- Water tank setup



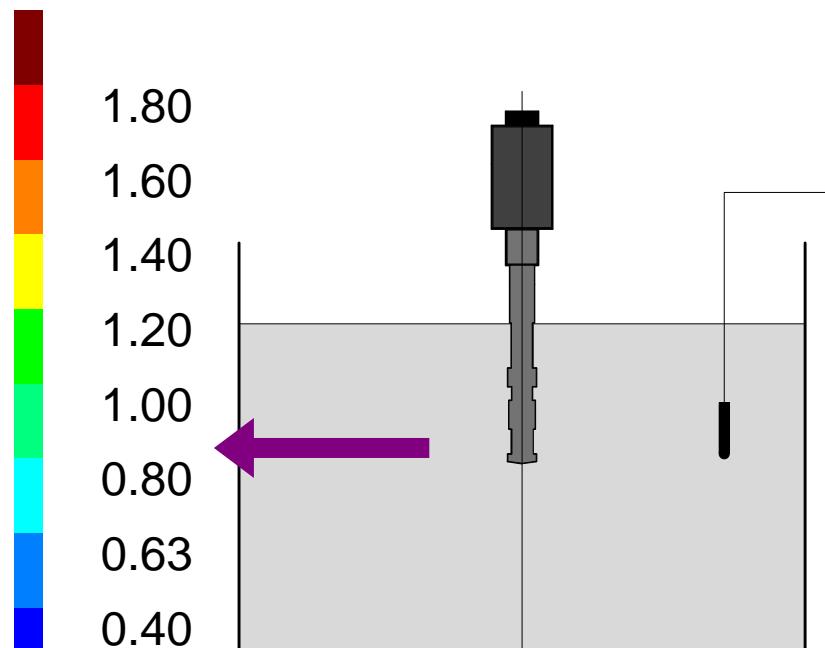
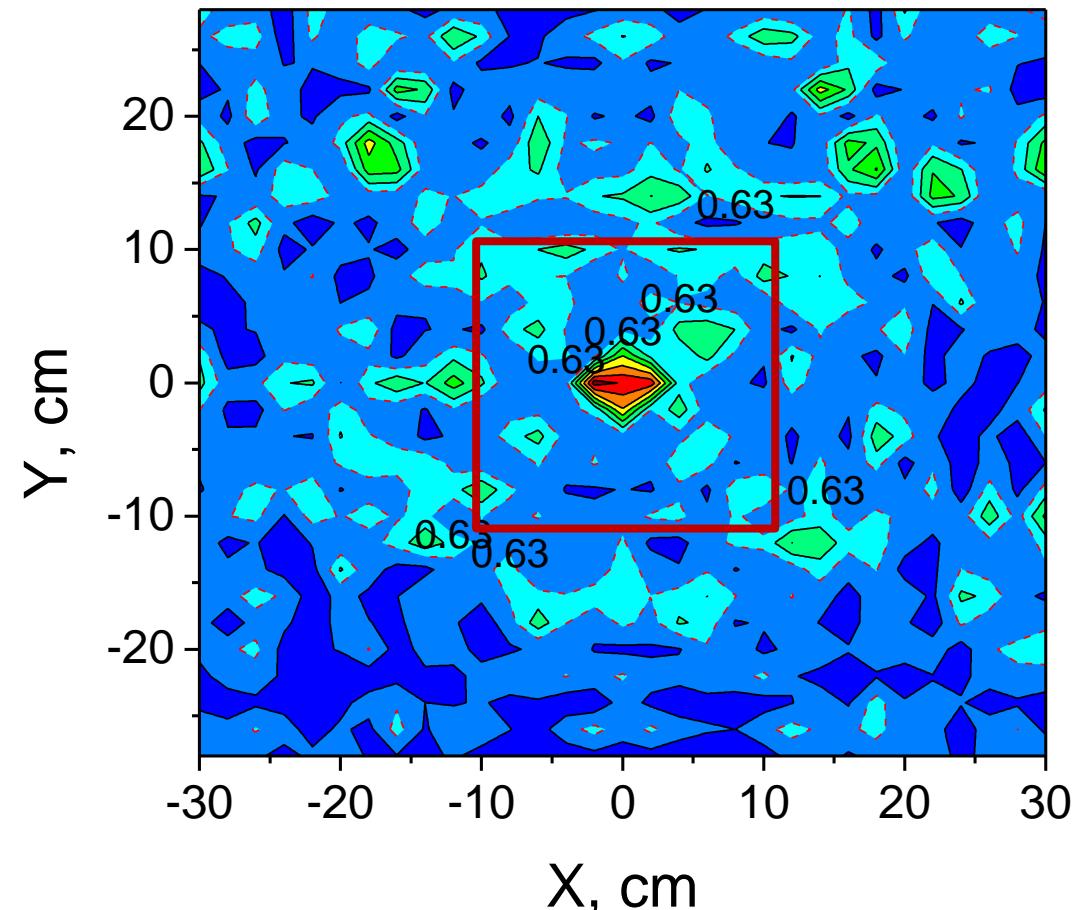
# Acoustic Field Mapping (X-Y Plane, Z=+4cm)

- Cavitation threshold (0.63V)
- Effective scale (~10cm)



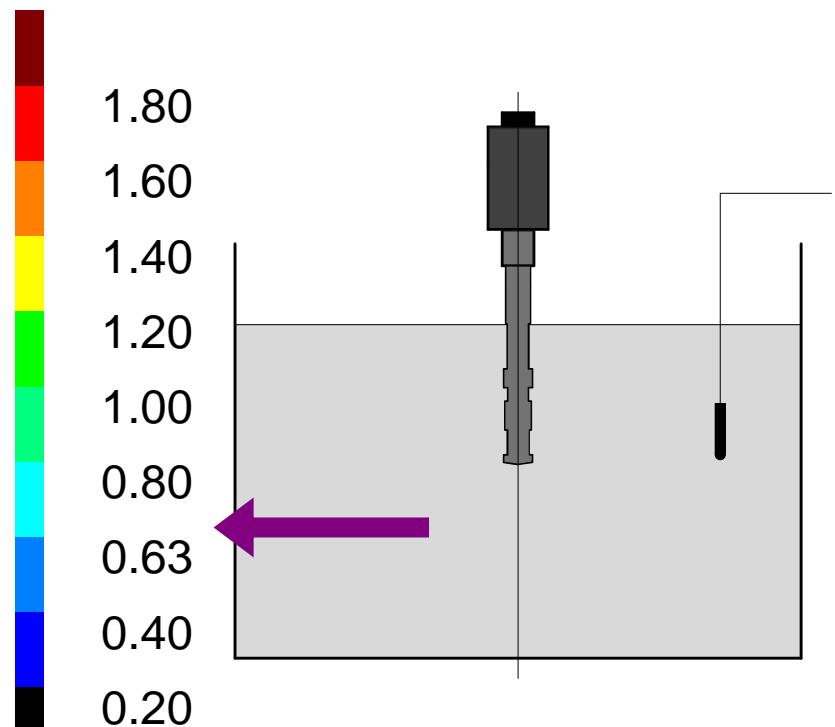
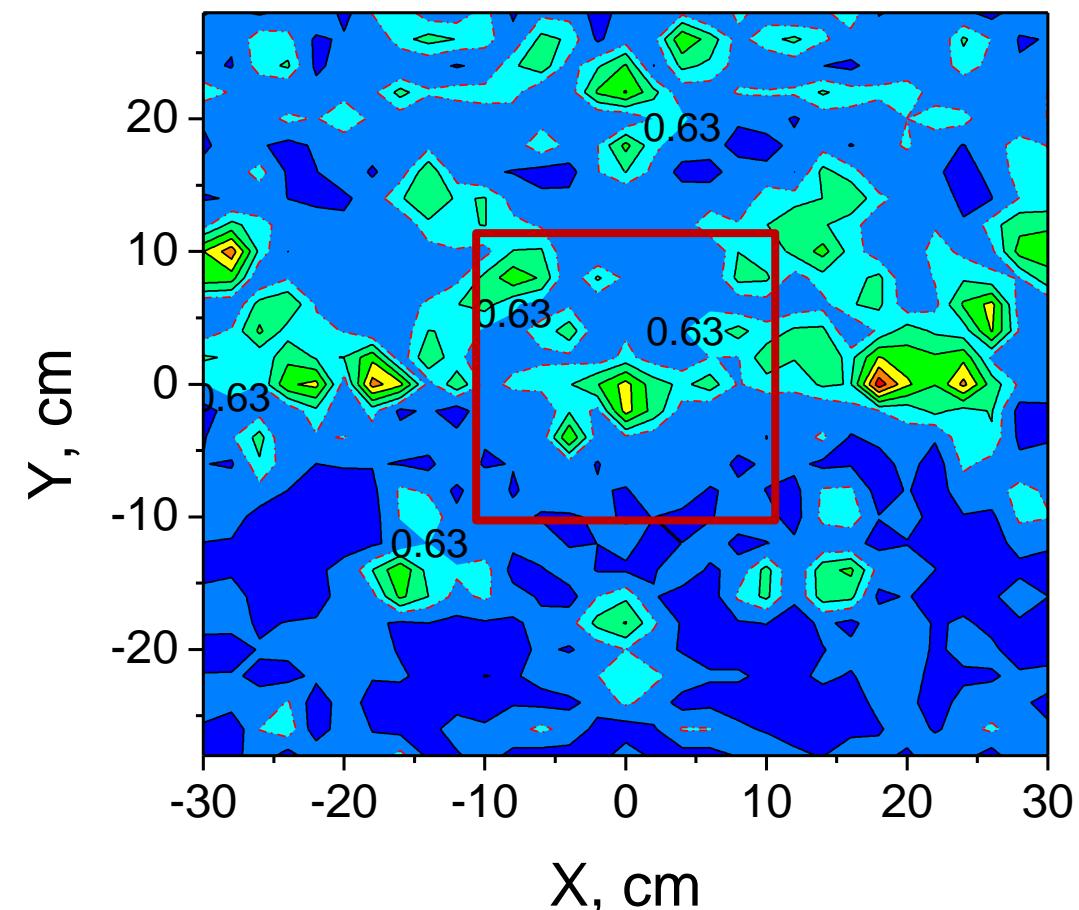
# Acoustic Field Mapping (X-Y Plane, Z=0cm)

- Cavitation threshold (0.63V)
- Effective scale (<10cm)



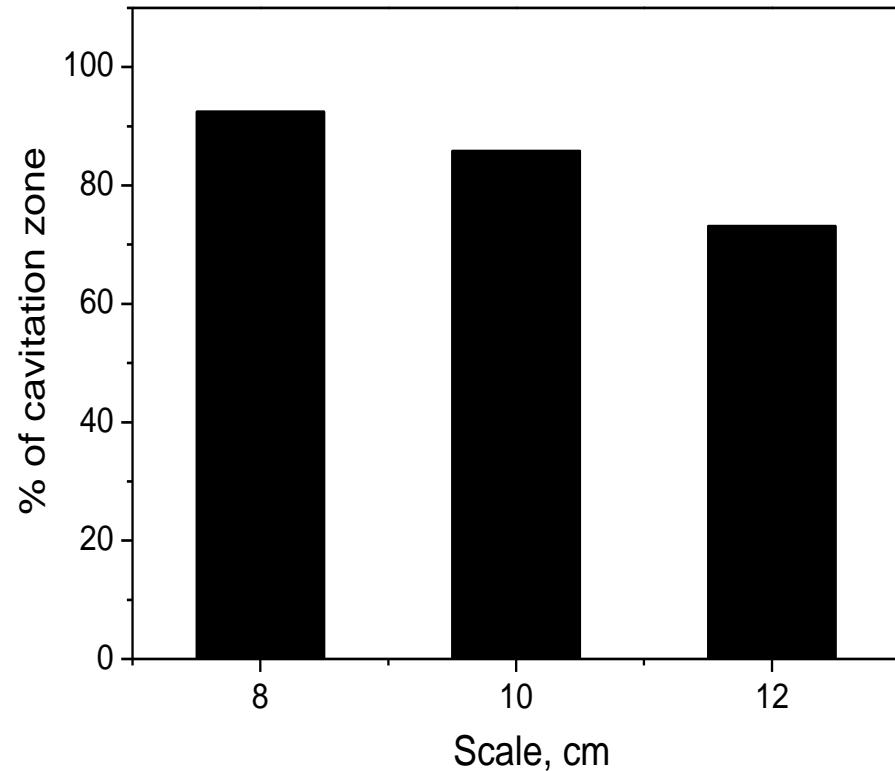
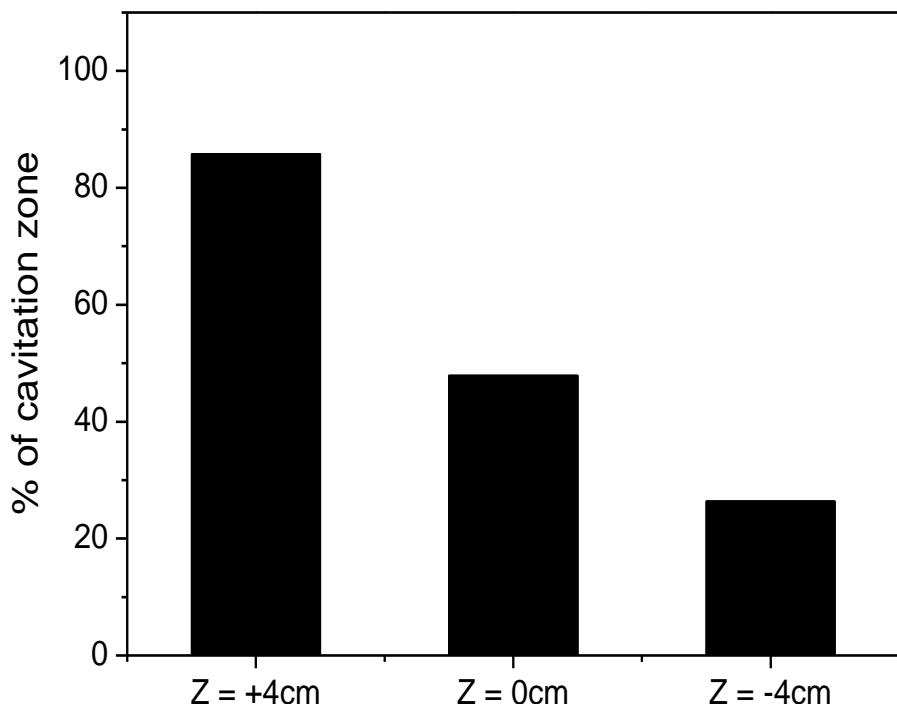
# Acoustic Field Mapping (X-Y Plane, Z=-4cm)

- Cavitation threshold (0.63V)
- Effective scale (<10cm)

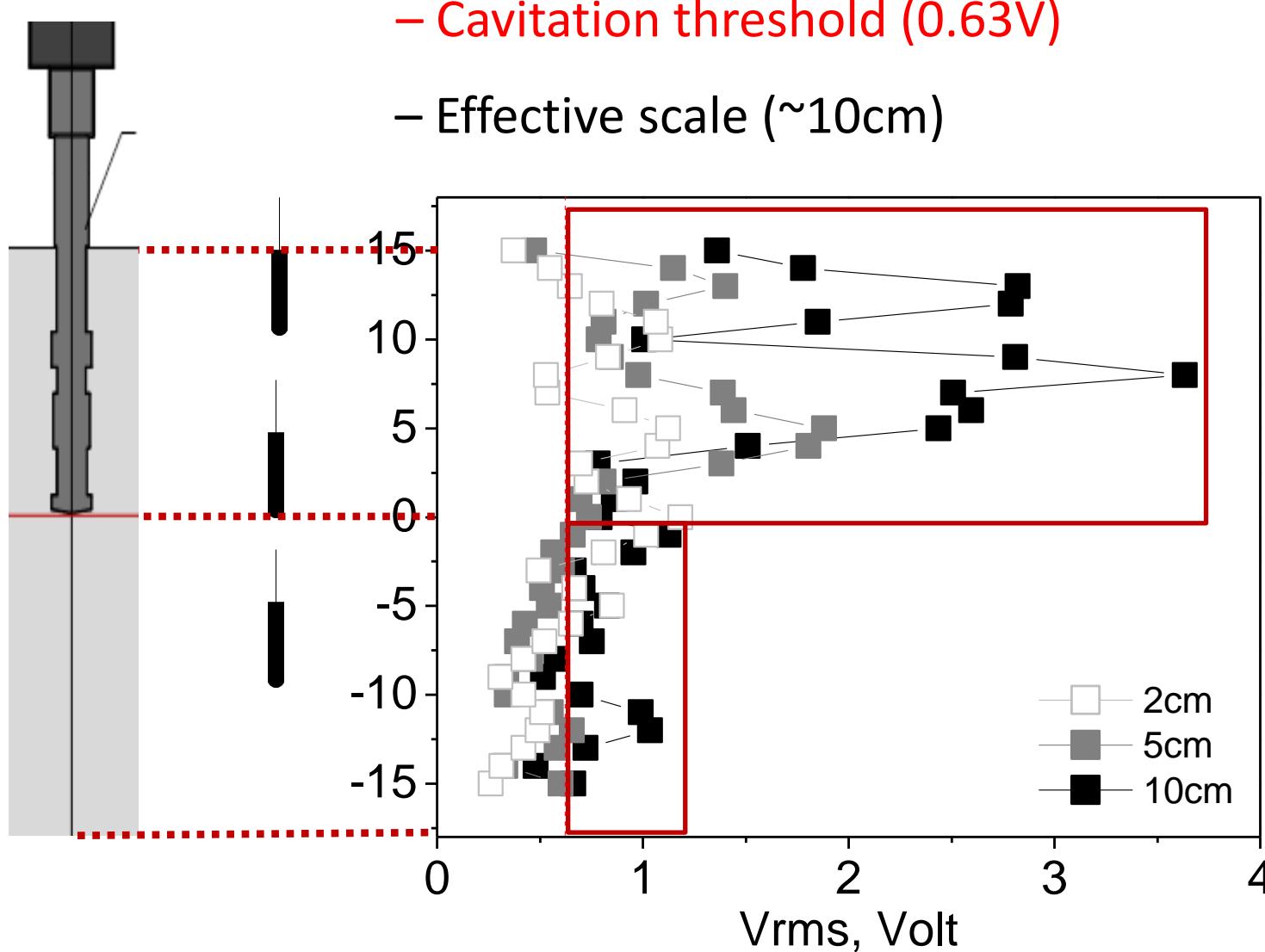


# Percentage of Cavitation Zone in X-Y Plane

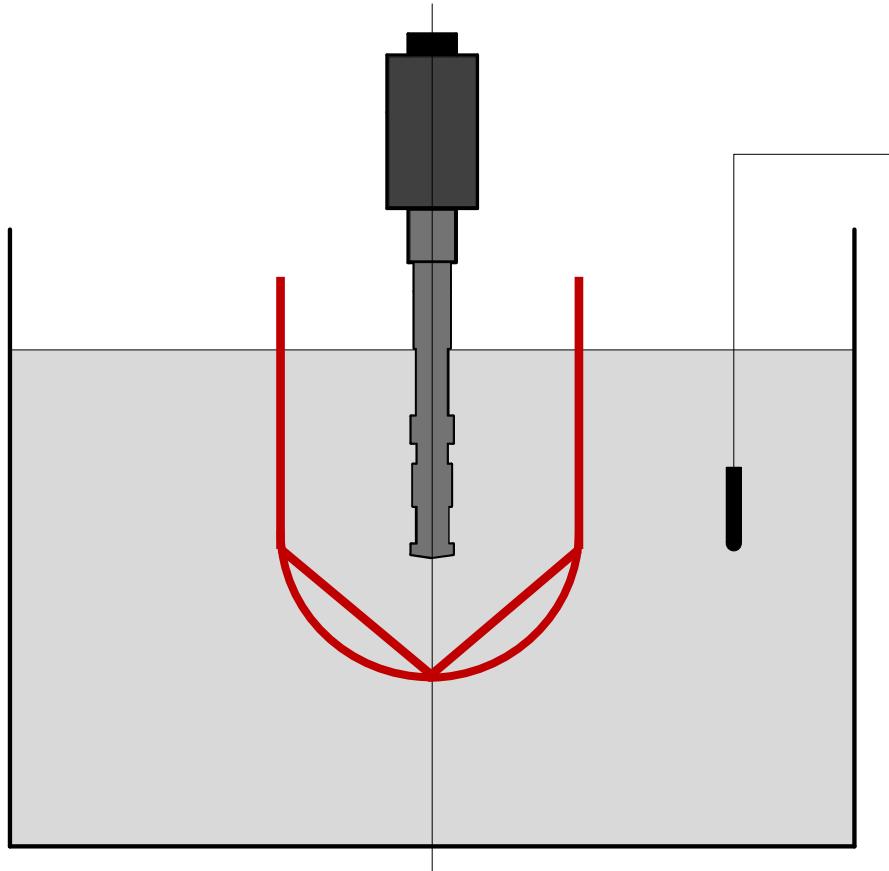
- Cavitation threshold (0.63V)
- Effective scale ( $\sim 10\text{cm}$ )



# Acoustic Field Mapping (Z-Direction)



# Reactor Configuration

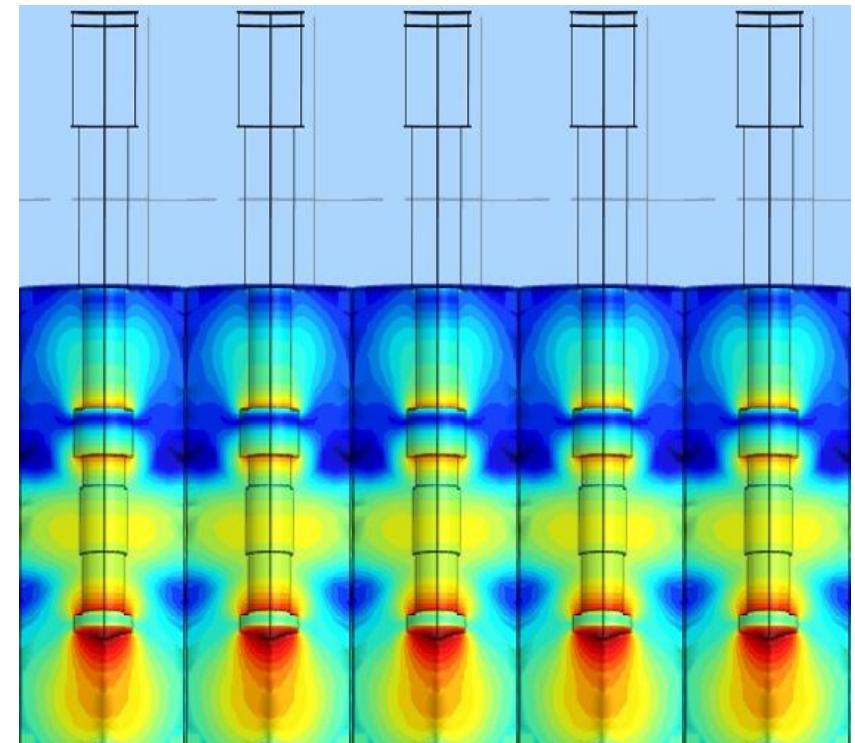


- Effective scale (10cm)
- Increase percentage of cavitation volume
- Treatment volume (~5.0L)



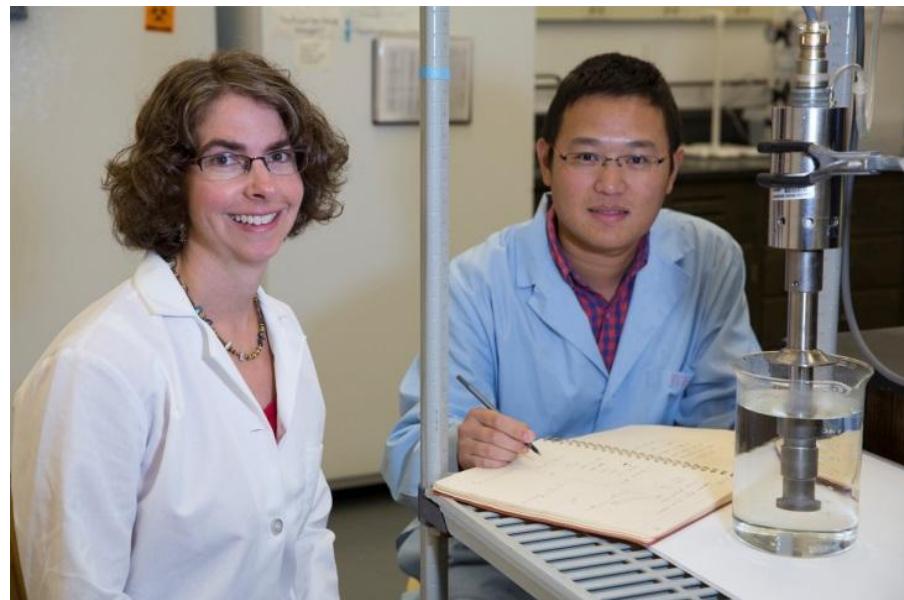
# Summary and Future Work

- Multi-stepped shape – more energy-emitting surfaces
- Hydrophone – design large sono-reactors
- Large-volume reactor
- Array of designed horns
- Synergistic effect



# Acknowledgement

- Dr. Linda Weavers
- James A Kosterman and ETREMA Products, Inc.
- Dr. Ruiyang Xiao, Dr. Meiqiang Cai, and Dr. Gim-Yang Pee

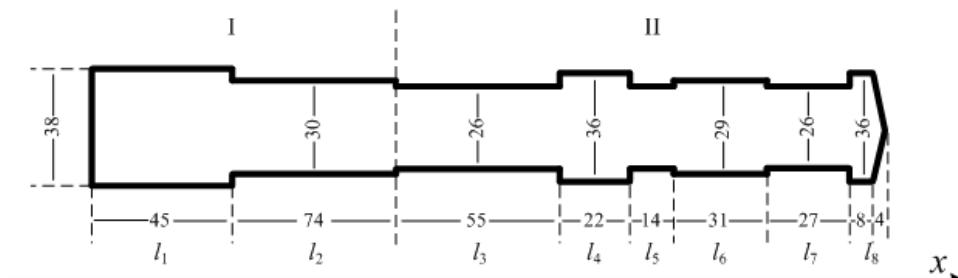
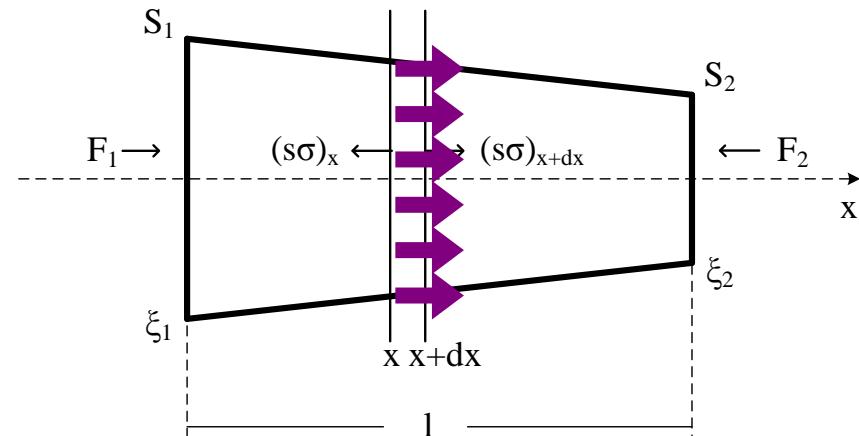


Thank You !

# Backup Slides

# Horn design requirements

- Resonance
  - *half-wave length*
  - $L=x \cdot (\lambda/2) = 280\text{mm}$
- Planar Homogeneous
  - $D < (\lambda/4) = 70\text{mm}$
- No concentrated energy
  - $M_p = 2.0$
- Multi-stepped shape
  - “edges”

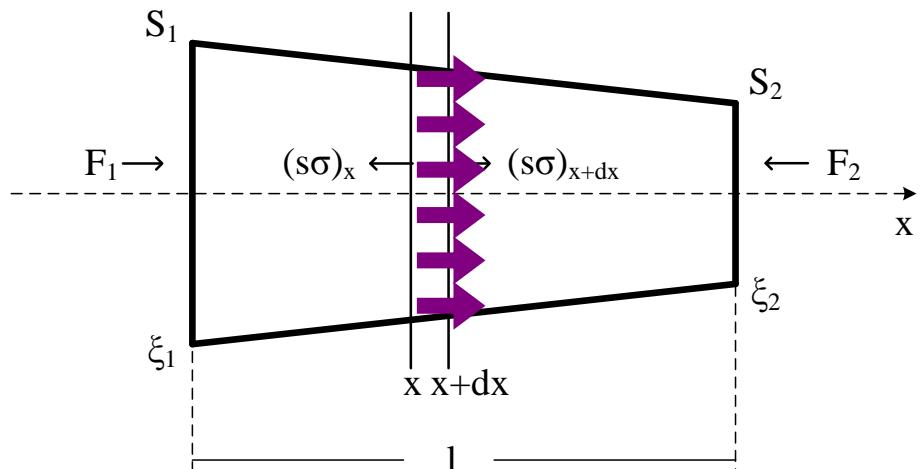


# Design Principles

- Dynamic wave equation

$$\frac{\partial(S \cdot \sigma)}{\partial x} dx = S \cdot \rho \frac{\partial^2 \xi}{\partial^2 t} dx$$

$$F = ma$$



- For a cylindrical horn in a steady-state mode

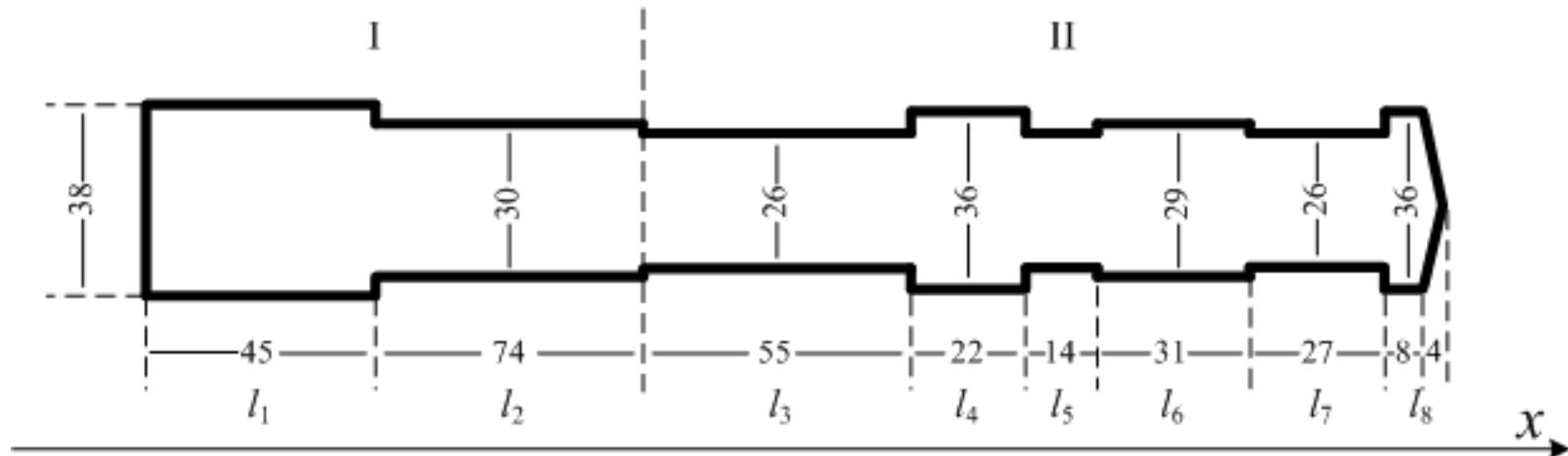
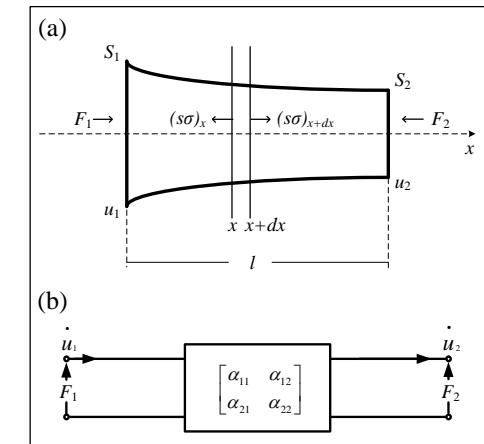
$$\frac{\partial^2 \xi}{\partial^2 x} + k^2 \xi = 0$$

# Design Principles

- Equivalent Circuit Model

$$\begin{bmatrix} \dot{u}_2 \\ F_2 \end{bmatrix} = \begin{bmatrix} \alpha_{11} & \alpha_{12} \\ \alpha_{21} & \alpha_{22} \end{bmatrix} \begin{bmatrix} \dot{u}_1 \\ F_1 \end{bmatrix}$$

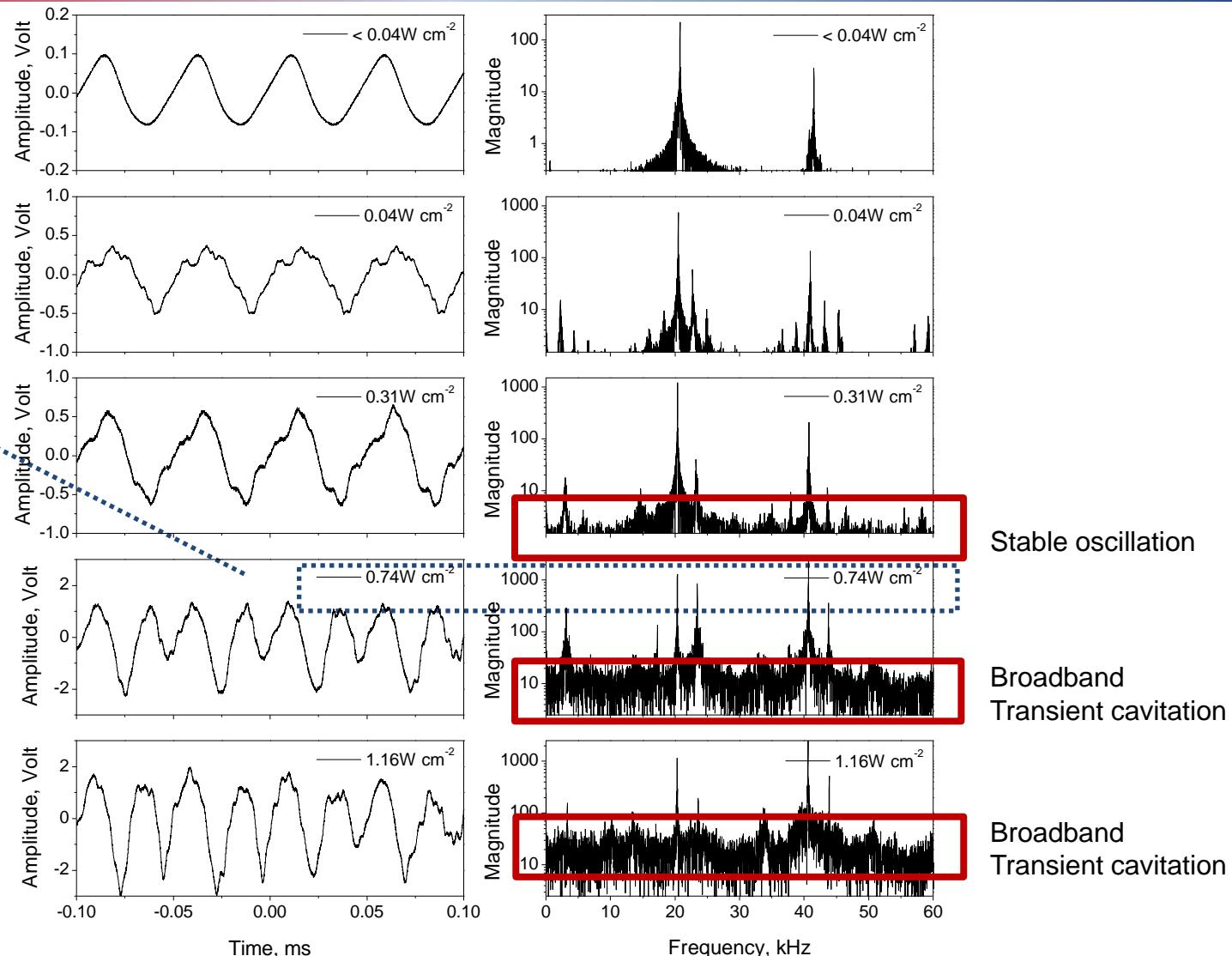
$$A = \begin{bmatrix} (\cos kl_8) & -j(\sin kl_8) \\ -j\rho c Si(\sin kl_8) & (\cos kl_8) \end{bmatrix} \dots \begin{bmatrix} (\cos kl_1) & -j(\sin kl_1) \\ -j\rho c Si(\sin kl_1) & (\cos kl_1) \end{bmatrix}$$



# Cavitation Threshold in Water

Threshold  
for bubble  
collapse!

0.63 Volt



Ultrasound waveforms and frequency spectrum observed from water at different power intensities

